

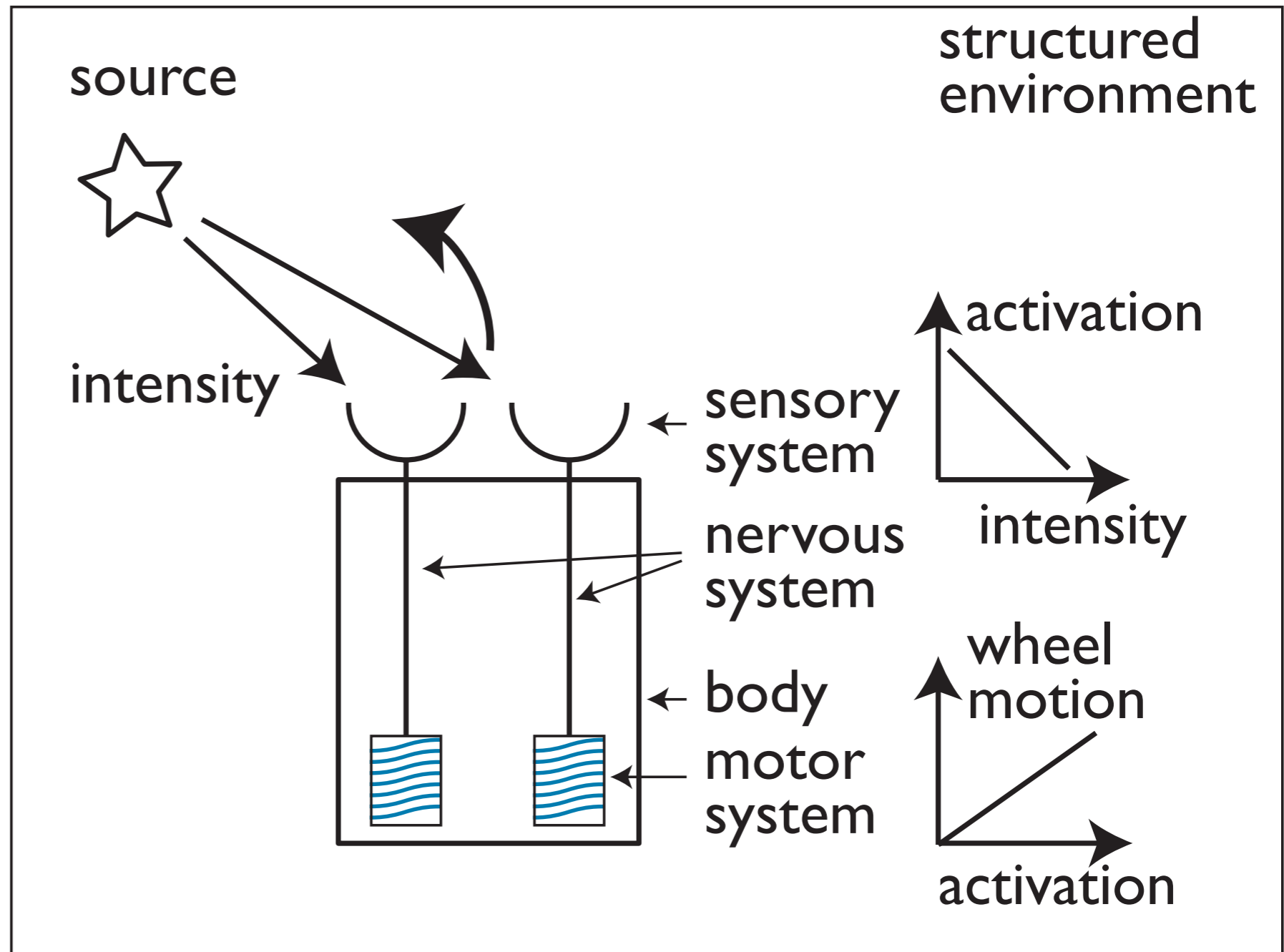
Summary

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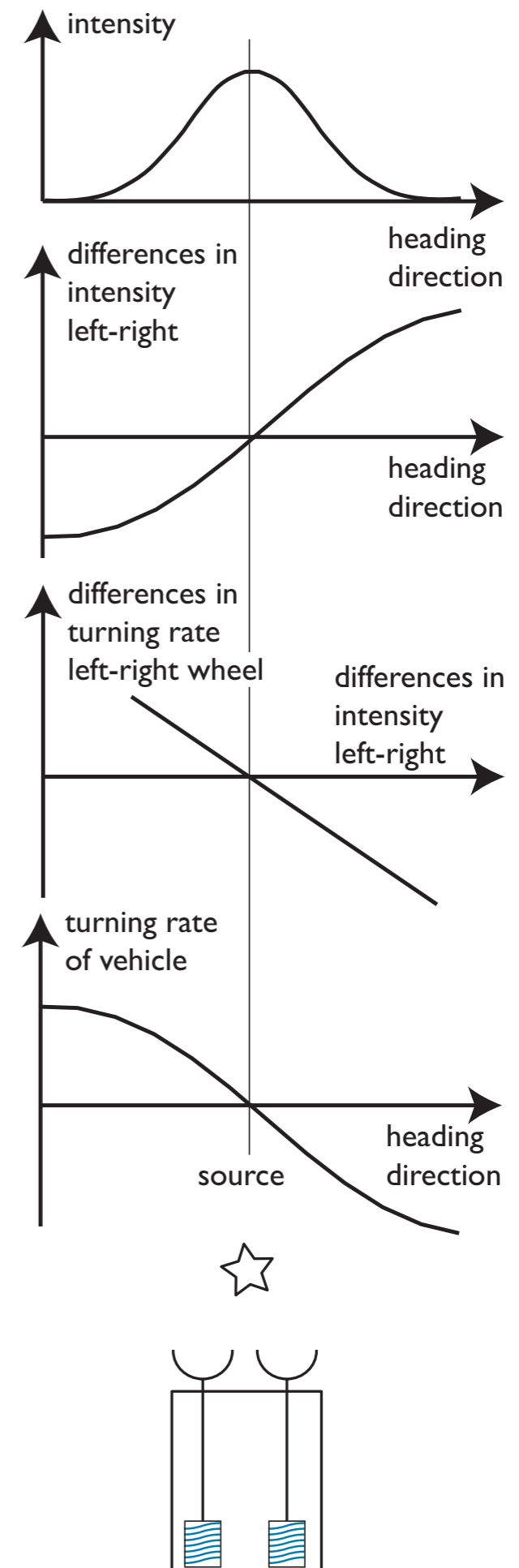
Five things needed to generate behavior

- sensors
- motors
- linked by a nervous system
- linked physically by a body
- an appropriately structured environment



Emergent behavior: this is a dynamics

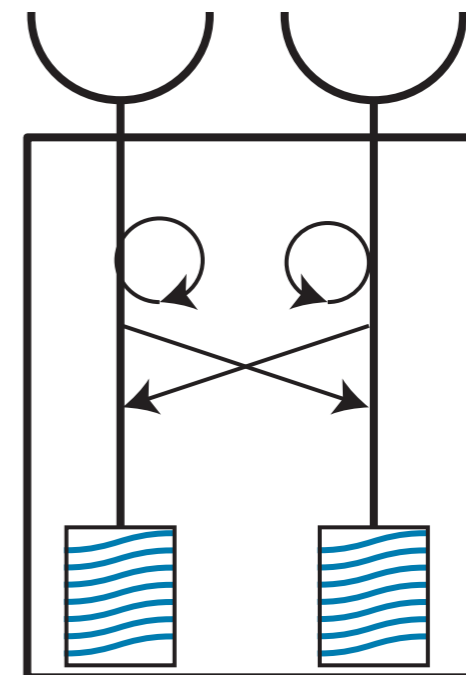
- feedforward nervous system
- + closed loop through environment
- => (behavioral) dynamics



Internal loops generate neural dynamics



- that generate cognition: internal decisions...
- bifurcations => different cognitive regimes

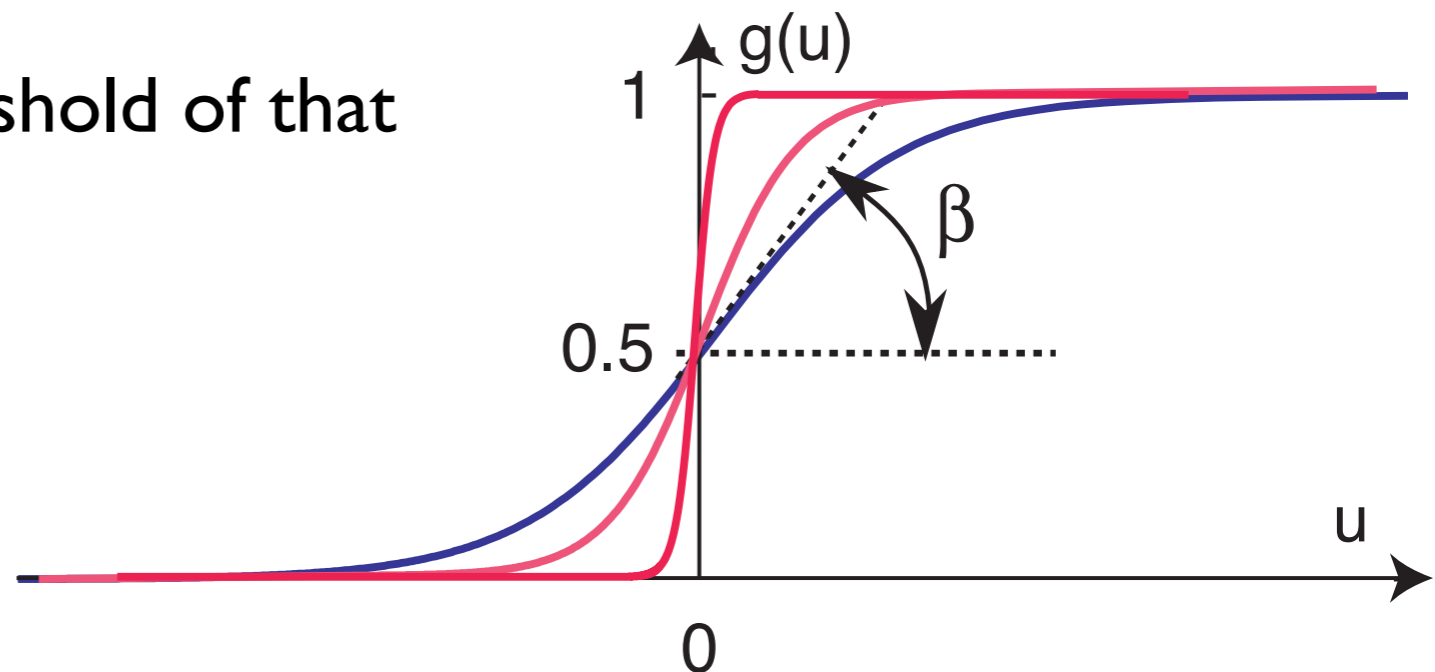


Activation

- **neural state variable activation**
 - linked to membrane potential of neurons in some accounts
 - linked to spiking rate in our account
 - through: population activation... (later)

Activation

- activation as a real number, abstracting from biophysical details
- low levels of activation: not transmitted to other systems (e.g., to motor systems)
- high levels of activation: transmitted to other systems
- as described by sigmoidal threshold function
- zero activation defined as threshold of that function

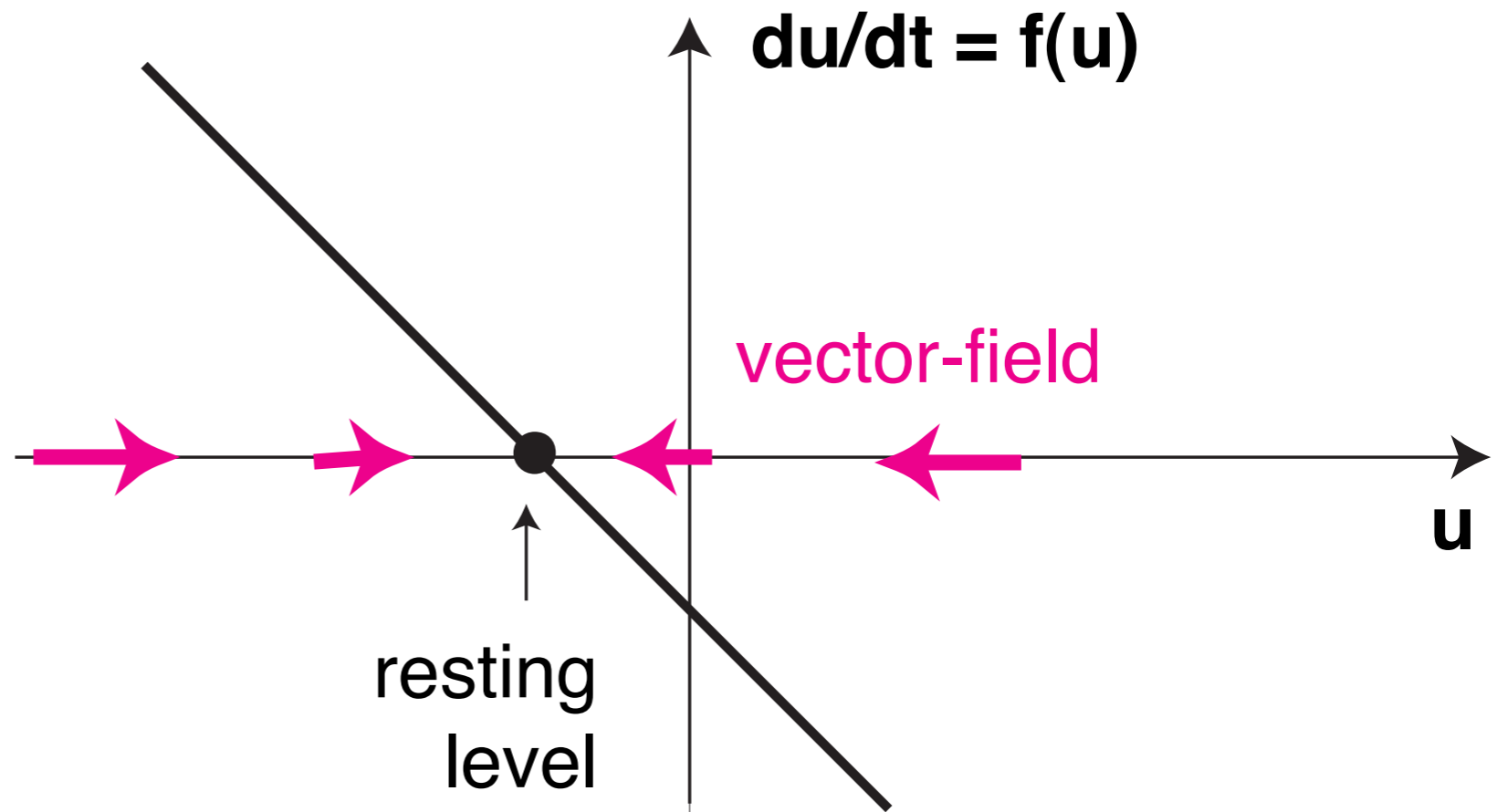


Activation dynamics

- activation evolves in continuous time
 - no evidence for a discretization of time, for spike timing to matter for behavior

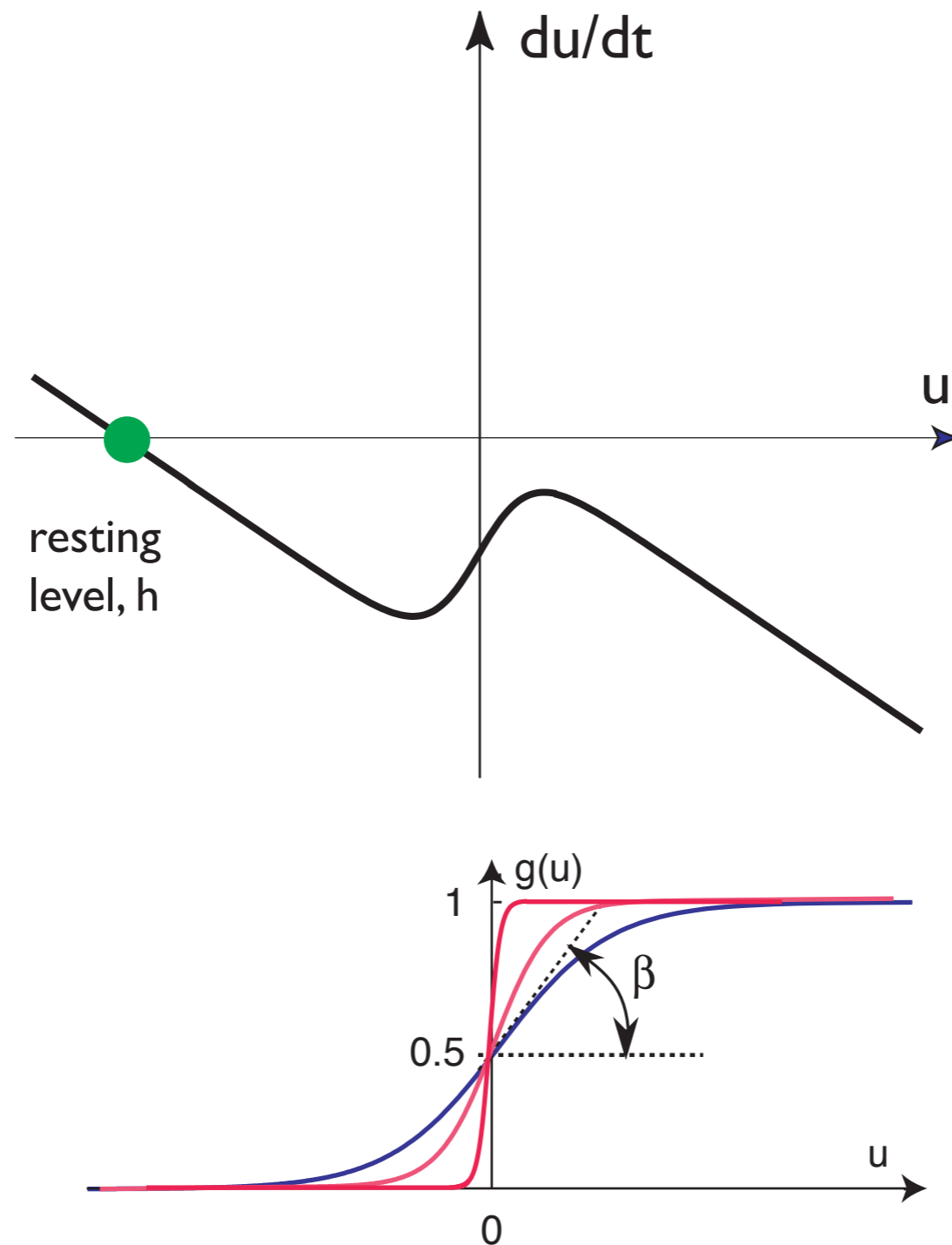
Neural dynamics

- stationary state=**fixed point**= constant solution
- stable fixed point: nearby solutions converge to the fixed point=**attractor**



$$\frac{du(t)}{dt} = \dot{u}(t) = -u(t) + h \quad (h < 0)$$

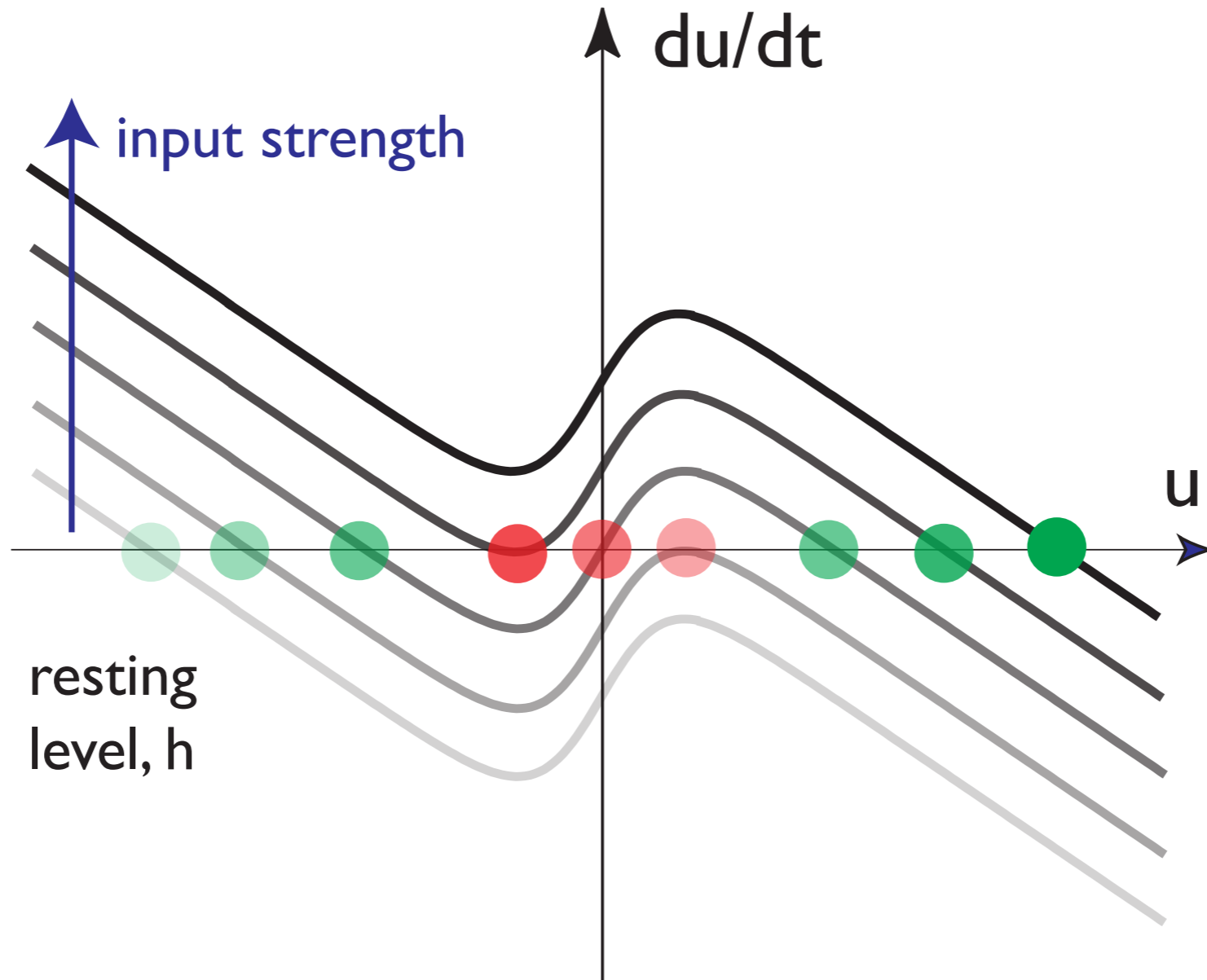
Neuronal dynamics with self-excitation



$$\tau \dot{u}(t) = -u(t) + h + S(t) + c\sigma(u(t))$$

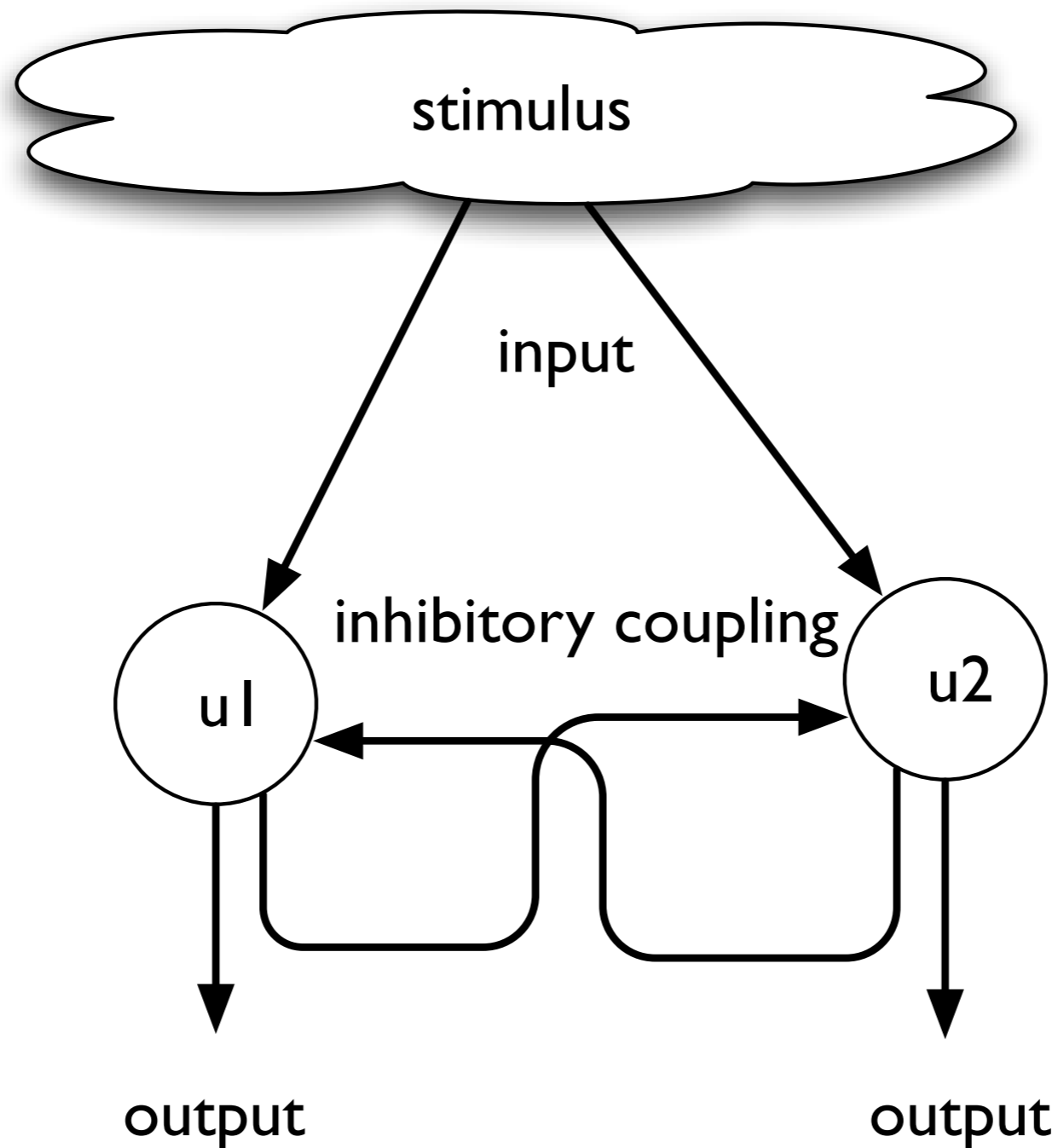
Neuronal dynamics with self-excitation

■ stimulus input



$$\tau \dot{u}(t) = -u(t) + h + S(t) + c\sigma(u(t))$$

Neuronal dynamics with competition

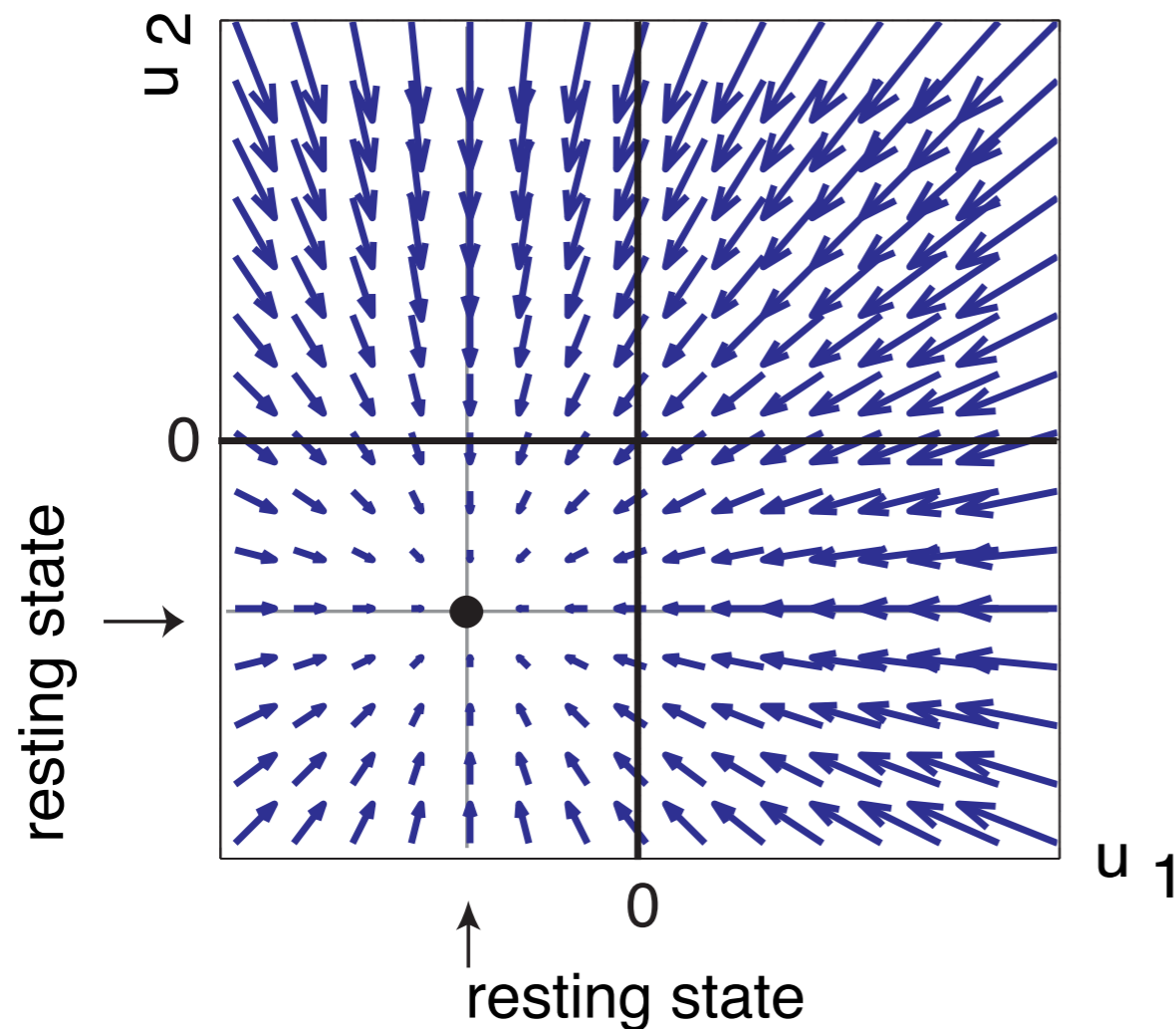


$$\tau \dot{u}_1(t) = -u_1(t) + h - \sigma(u_2(t)) + S_1$$

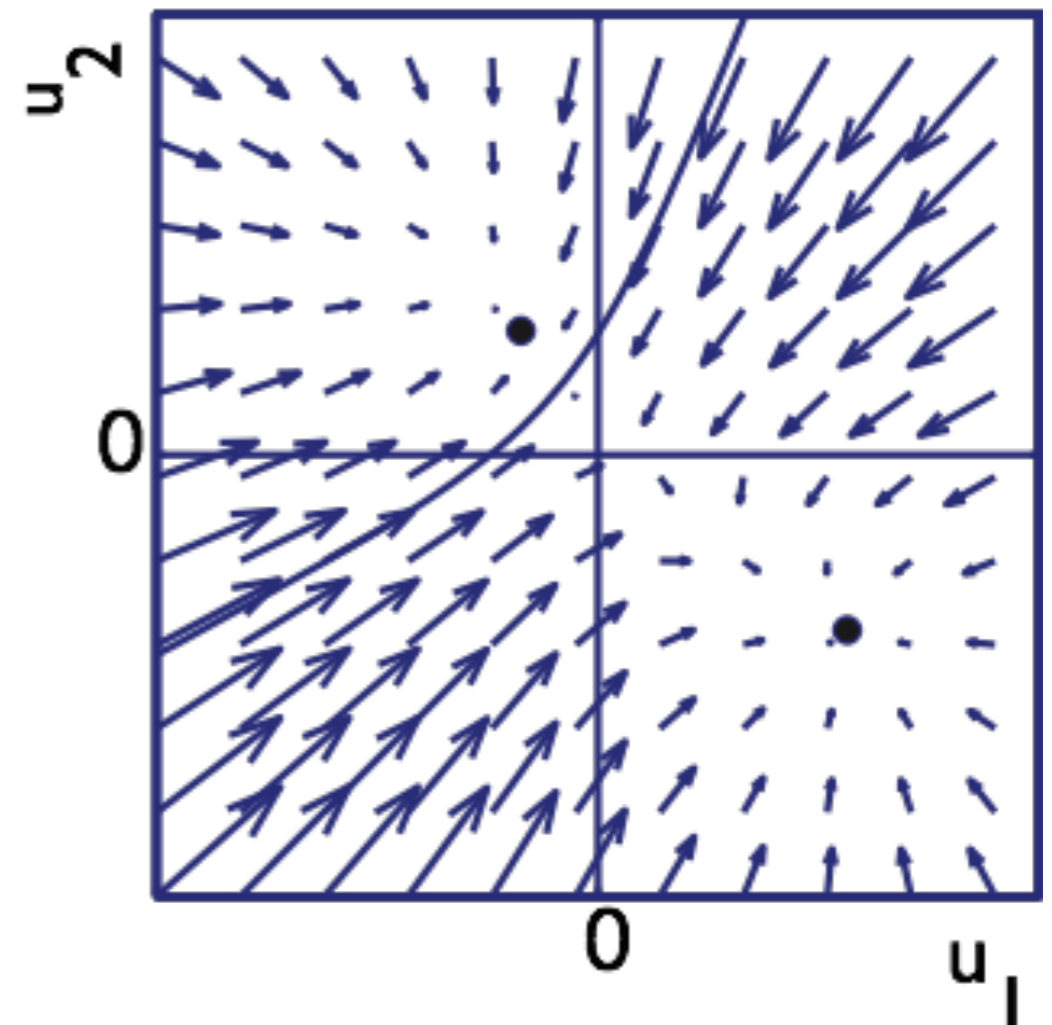
$$\tau \dot{u}_2(t) = -u_2(t) + h - \sigma(u_1(t)) + S_2$$

Neuronal dynamics with competition => biased competition

before input is presented

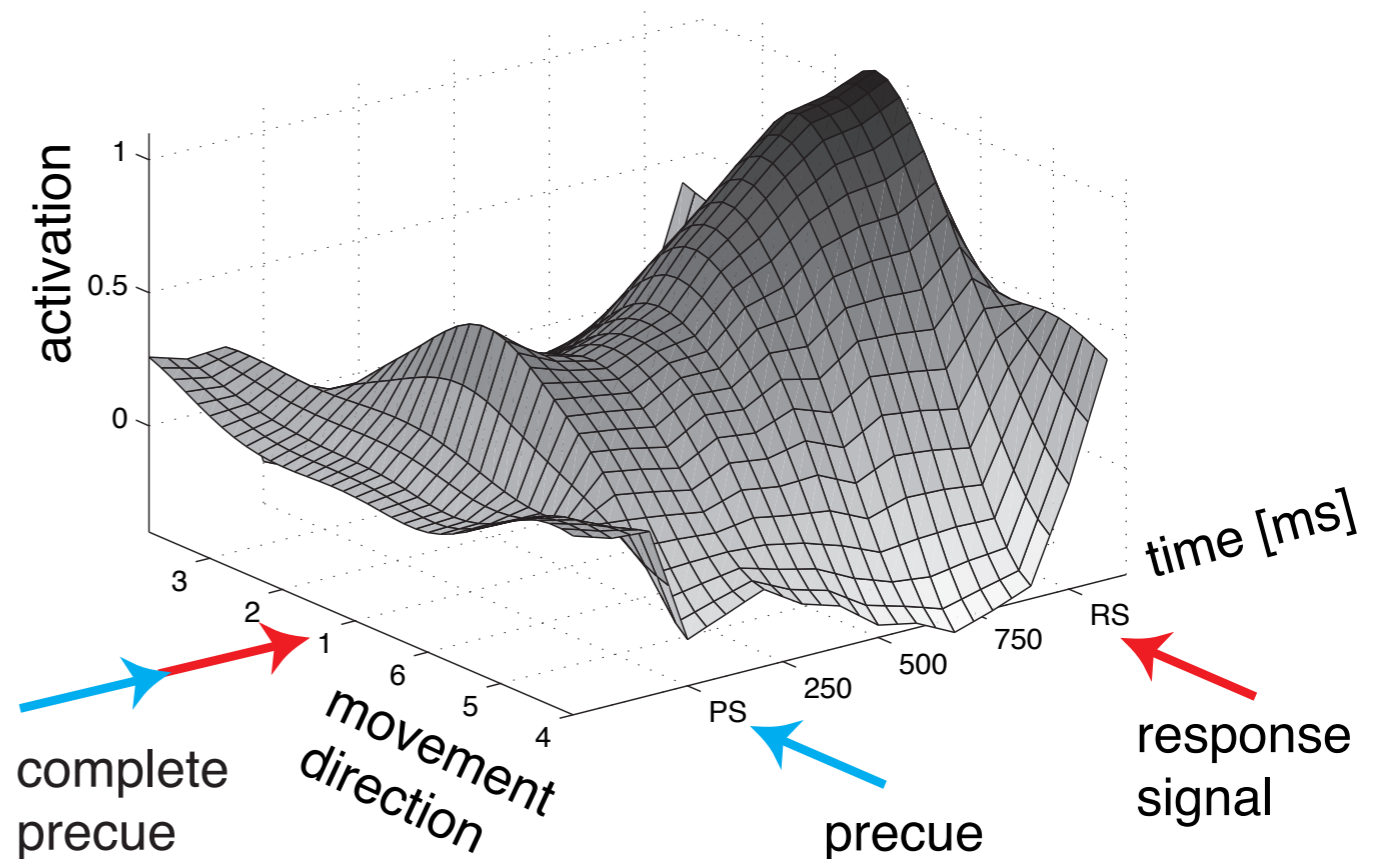
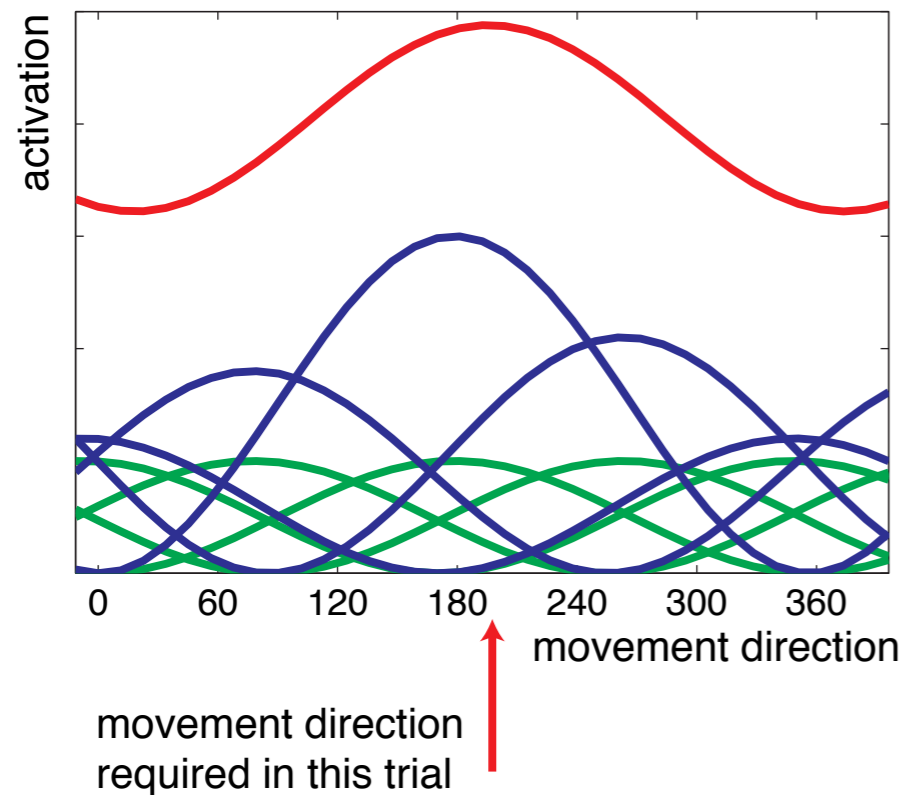


after input is presented



Distribution of Population Activation (DPA)

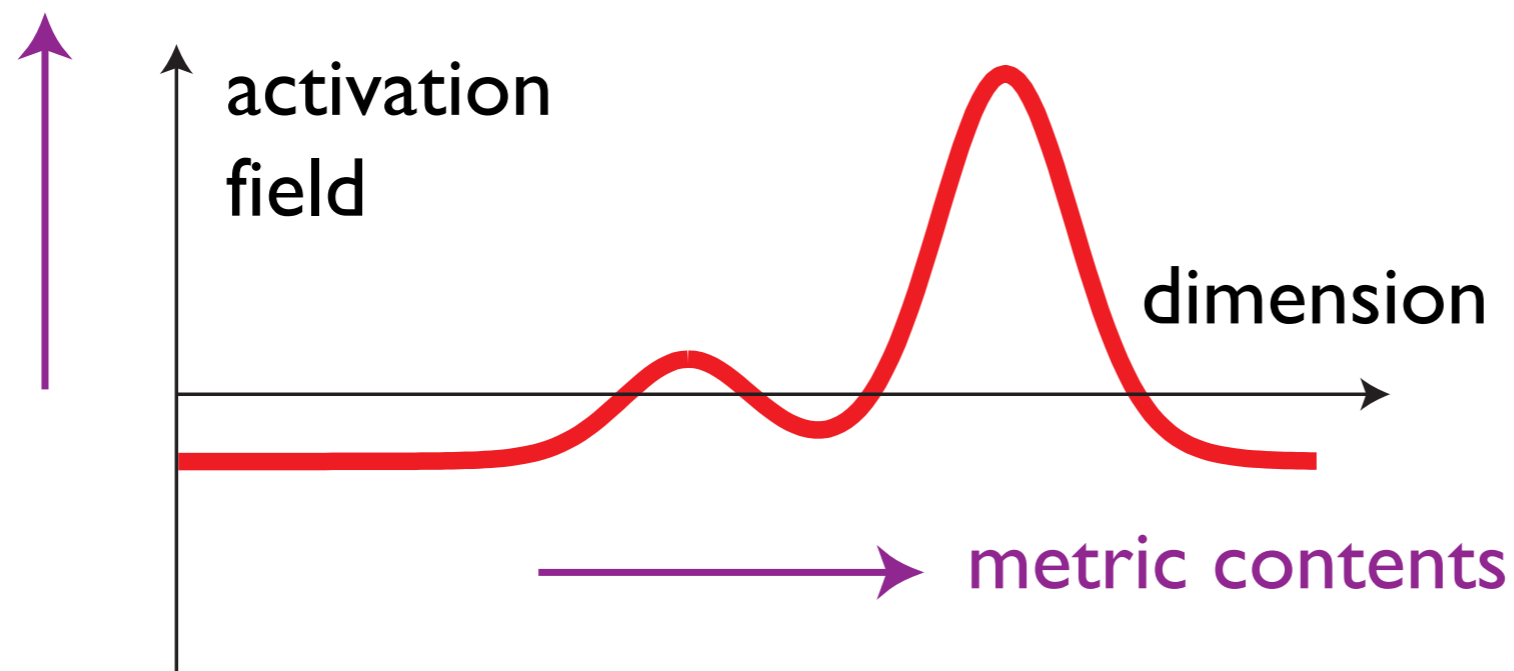
Distribution of population activation =
 $\sum_{\text{neurons}} \text{tuning curve} * \text{current firing rate}$



Dynamical Field Theory: space

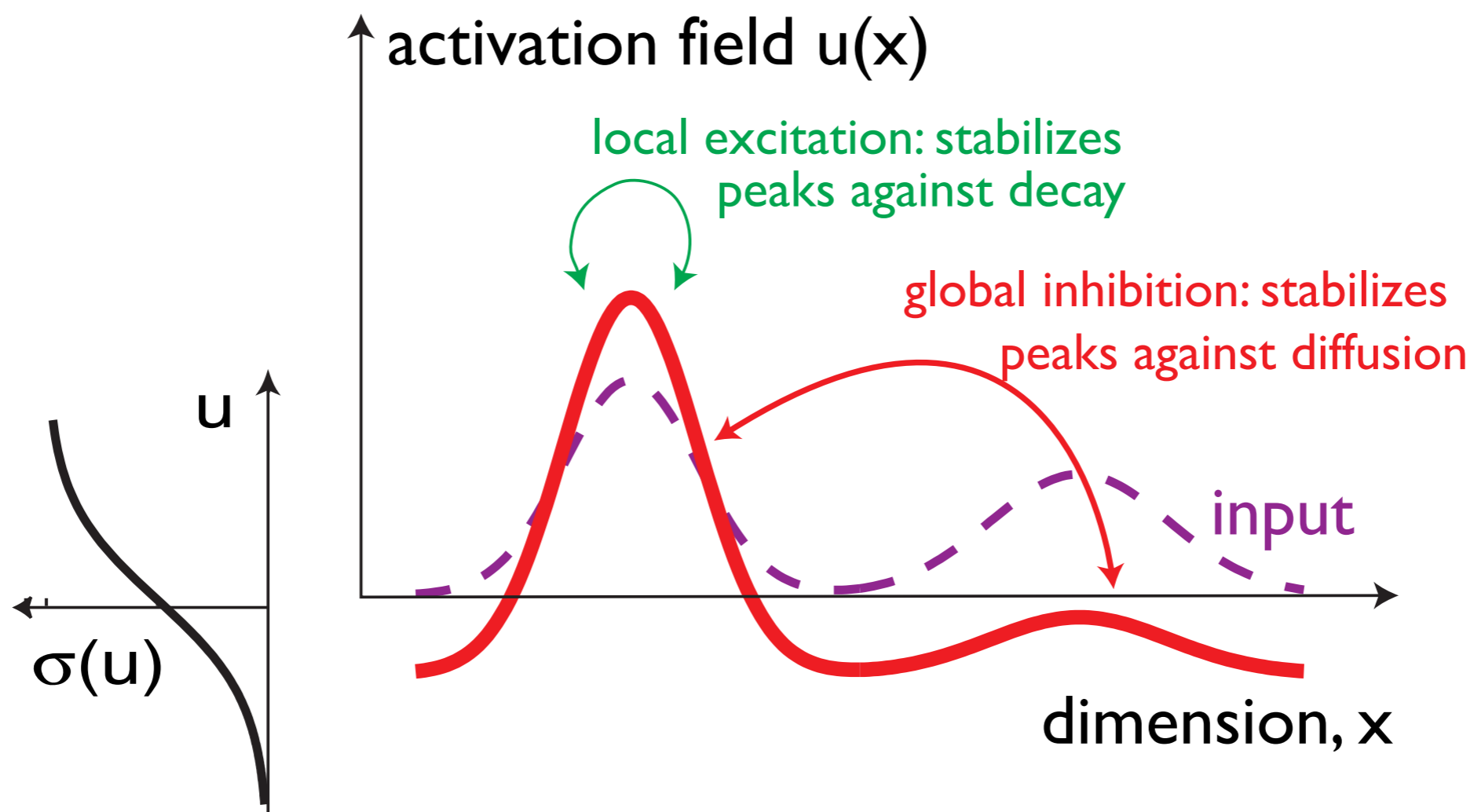
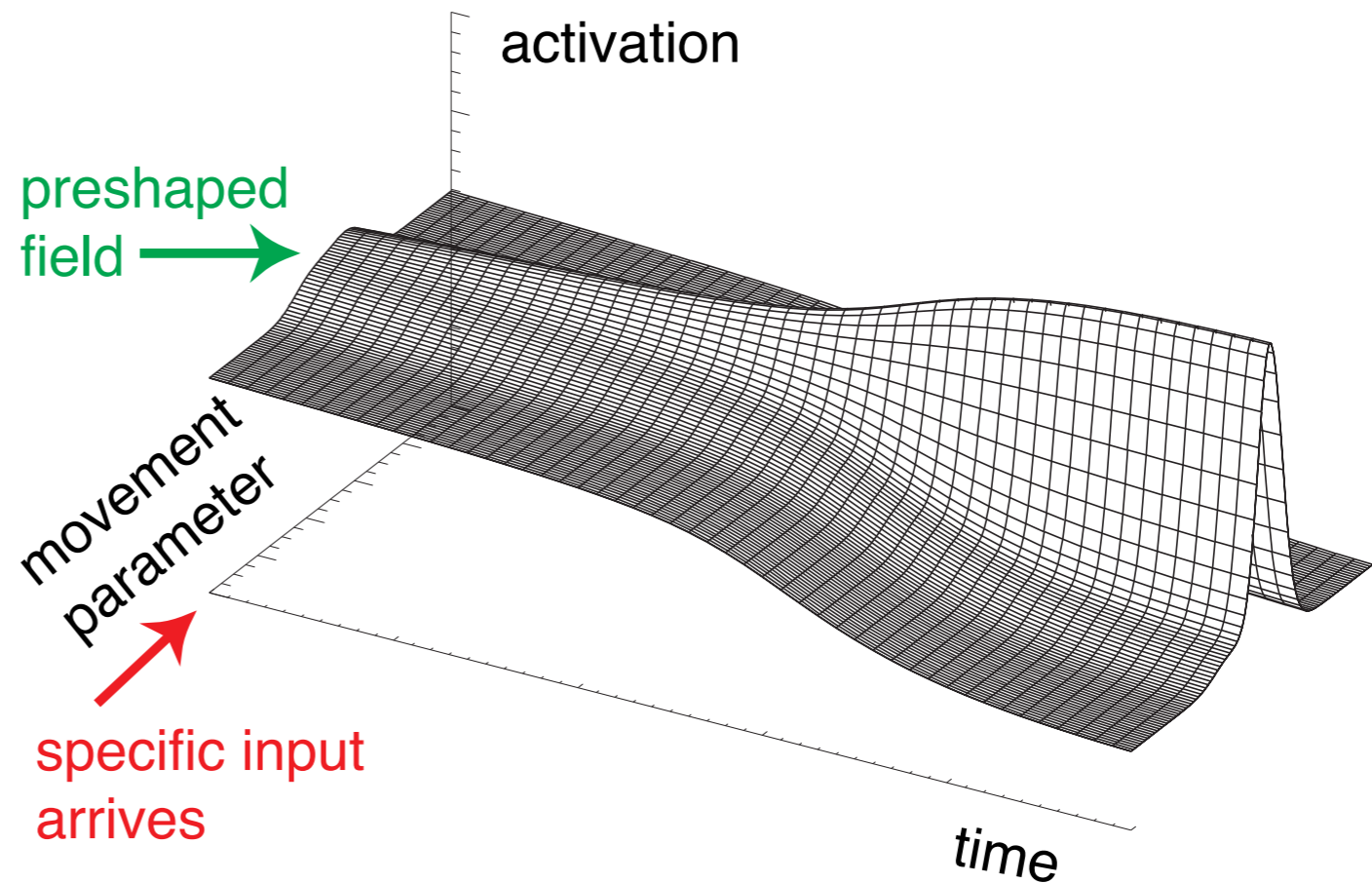
- fields: continuous activation variables defined over continuous spaces

information, probability, certainty



e.g., retinal space, movement parameters, feature dimensions, viewing parameters, ...

the dynamics such as activation fields is structured so that localized peaks emerge as attractor solutions



mathematical formalization

Amari equation

$$\tau \dot{u}(x, t) = -u(x, t) + h + S(x, t) + \int w(x - x') \sigma(u(x', t)) dx'$$

where

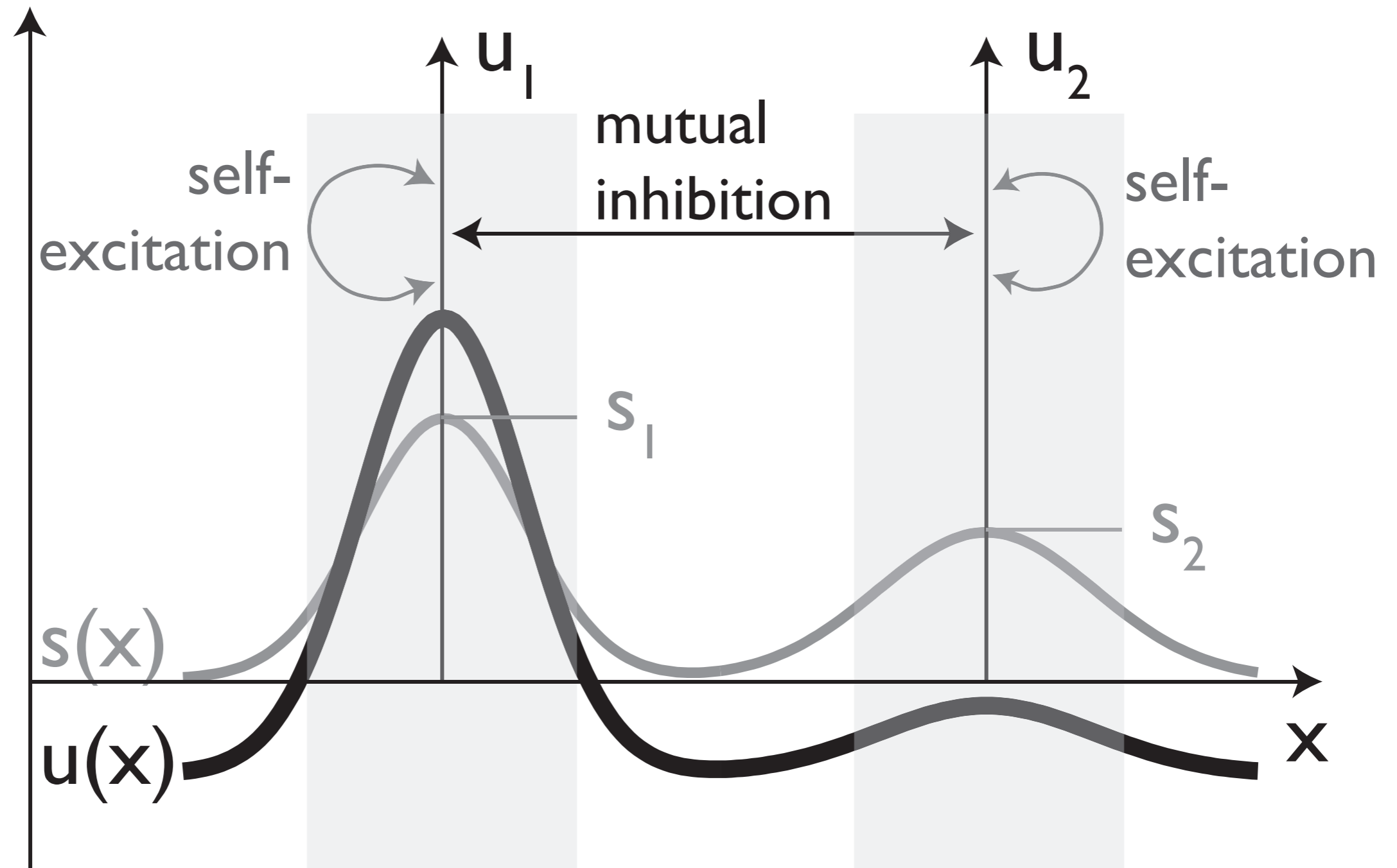
- time scale is τ
- resting level is $h < 0$
- input is $S(x, t)$
- interaction kernel is

$$w(x - x') = w_i + w_e \exp \left[-\frac{(x - x')^2}{2\sigma_i^2} \right]$$

- sigmoidal nonlinearity is

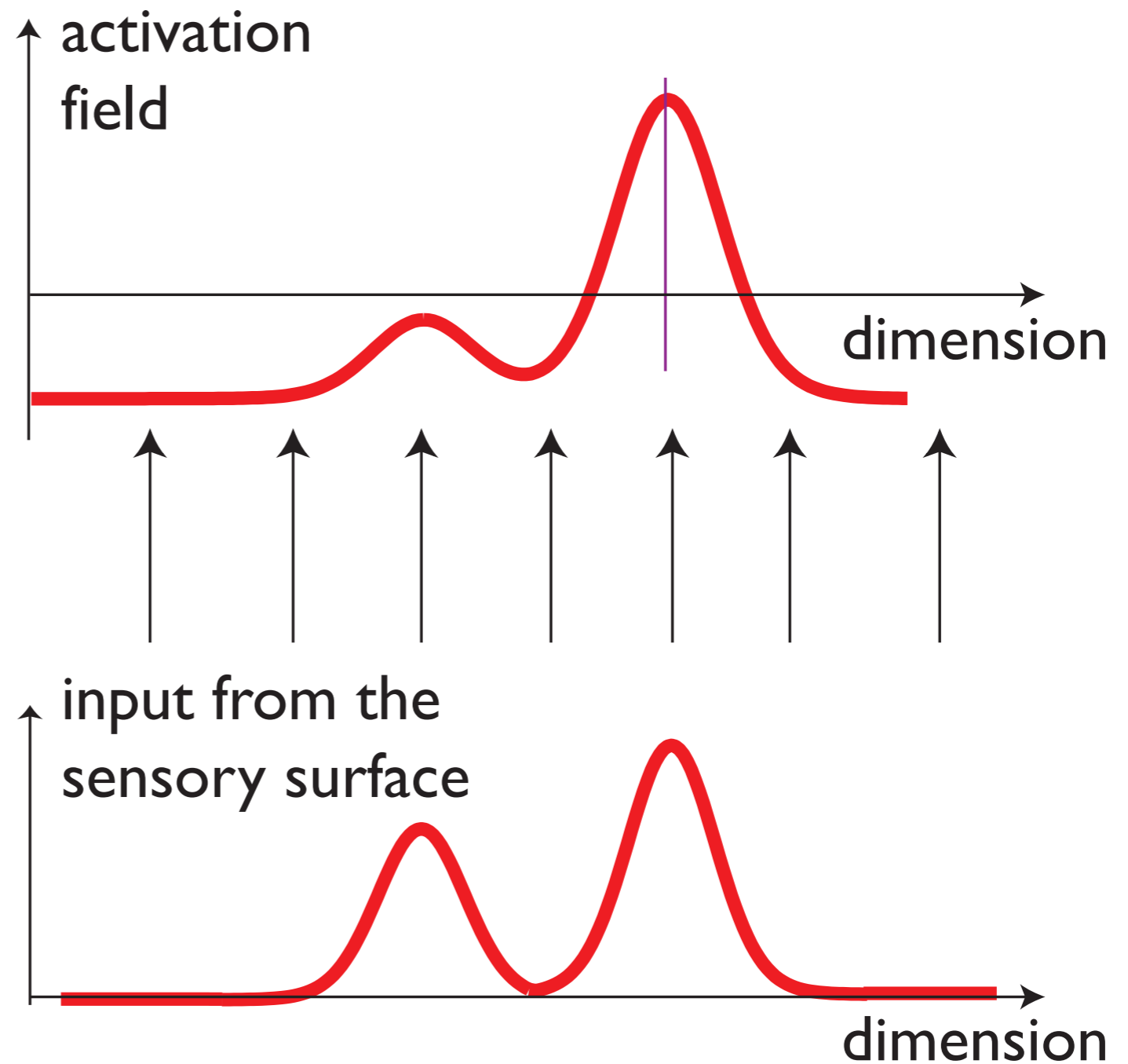
$$\sigma(u) = \frac{1}{1 + \exp[-\beta(u - u_0)]}$$

Relationship to the dynamics of discrete activation variables

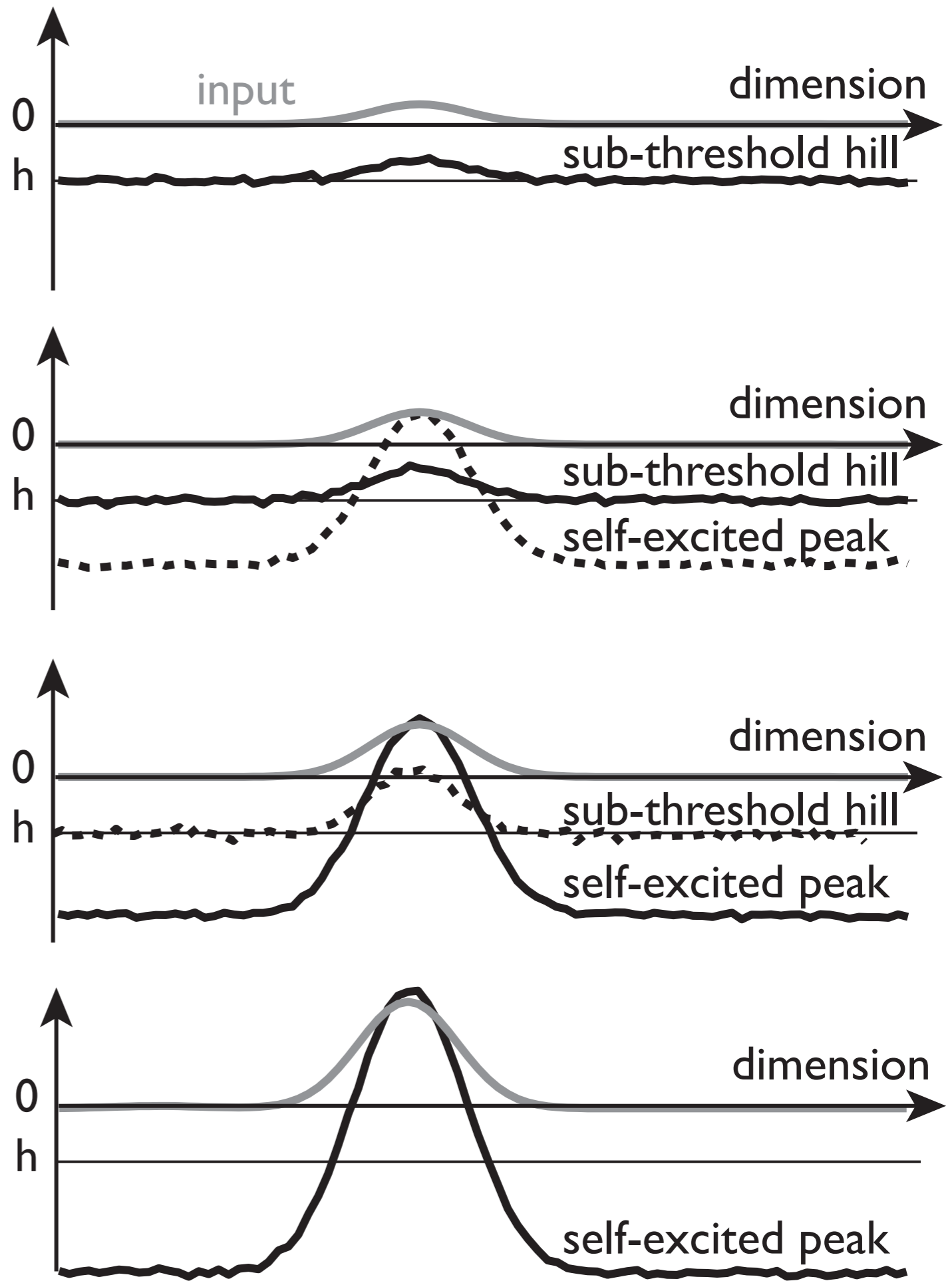


How does a field come to stand for “its” dimension?

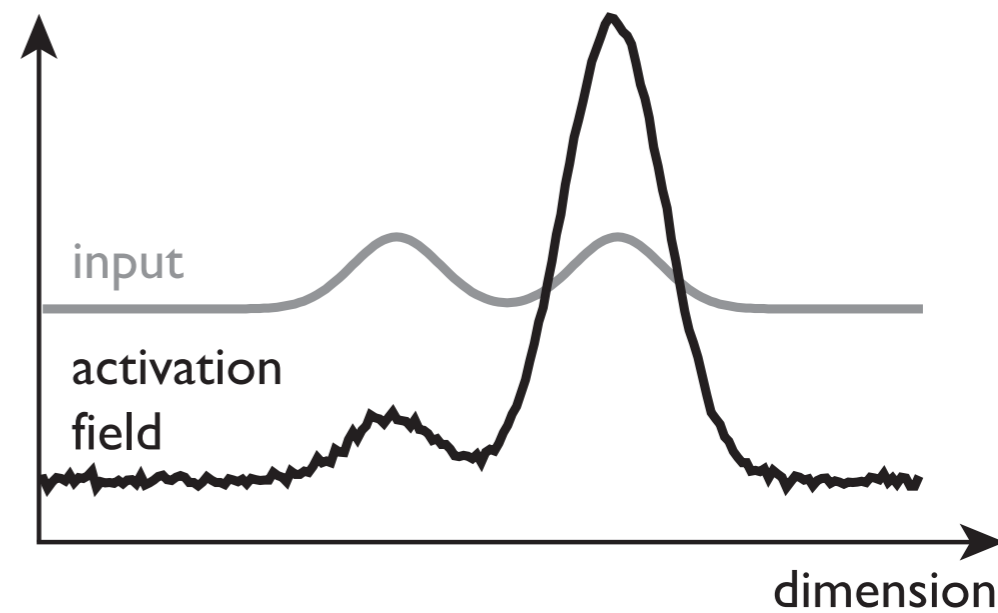
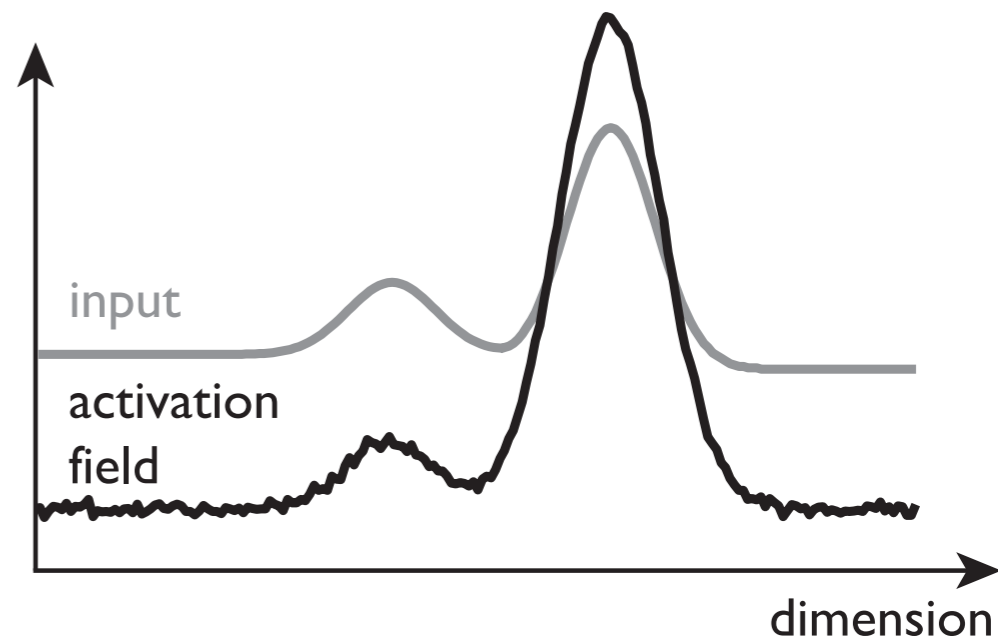
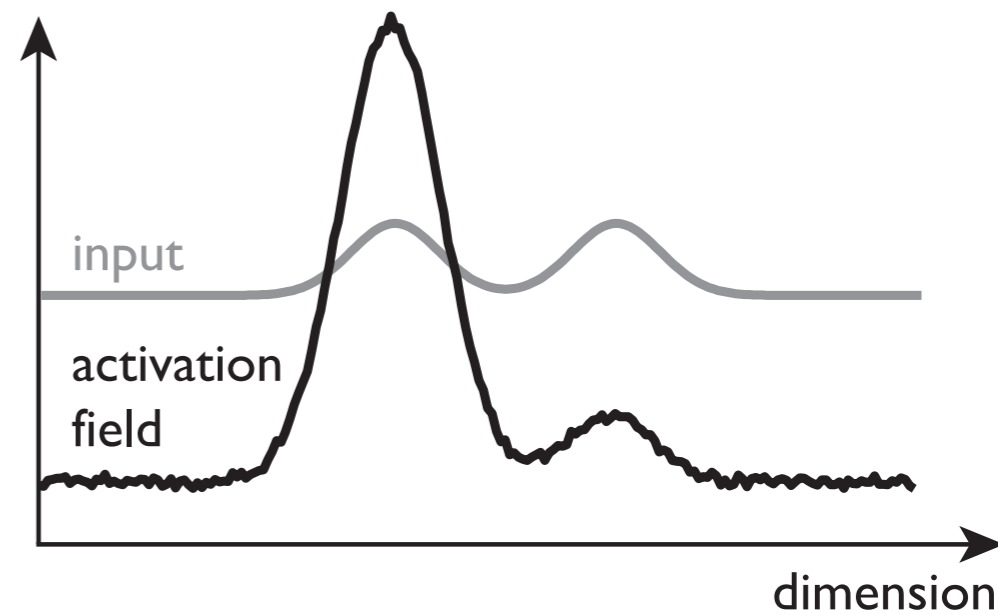
■ => by its input/output connectivity...



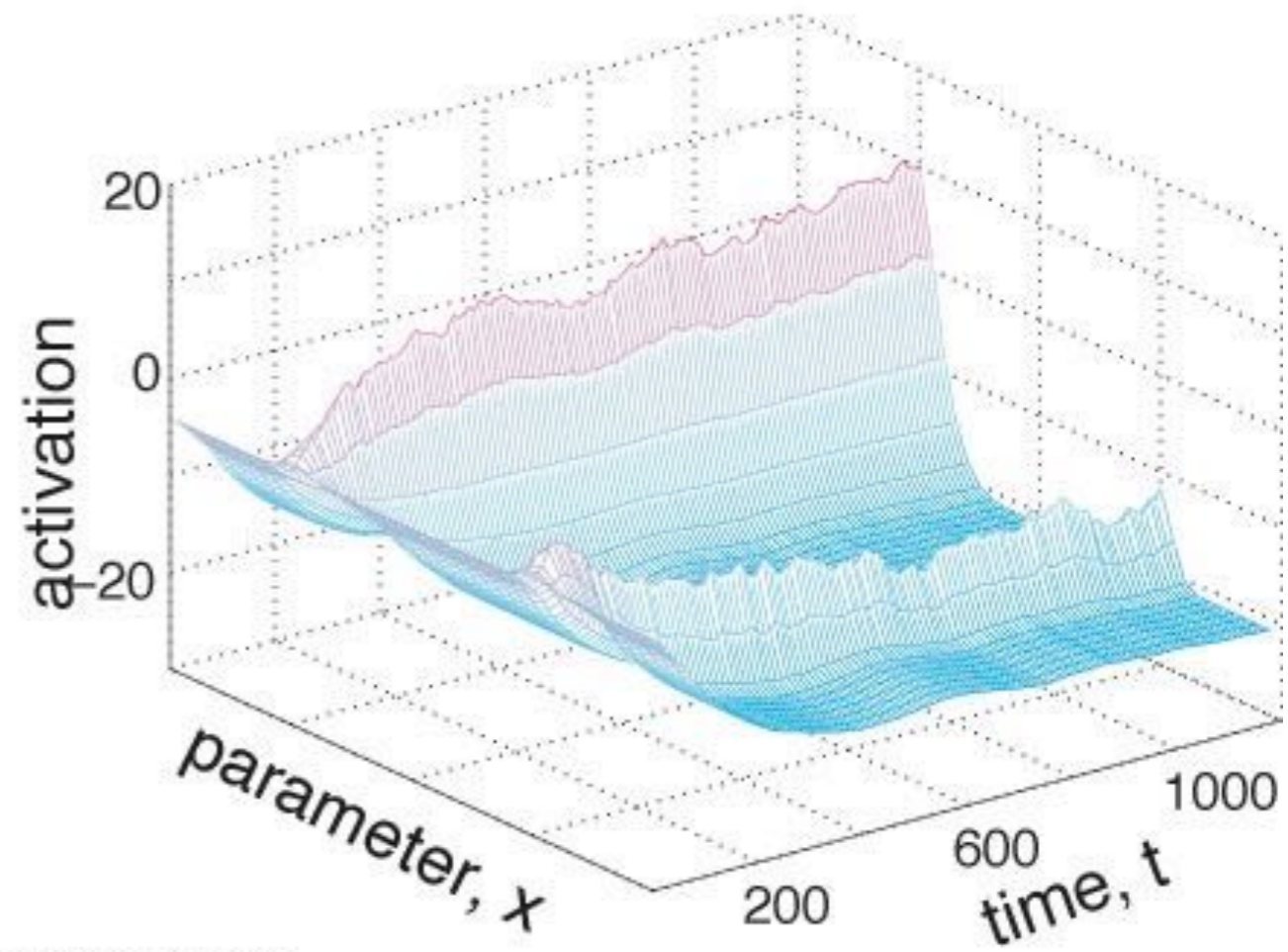
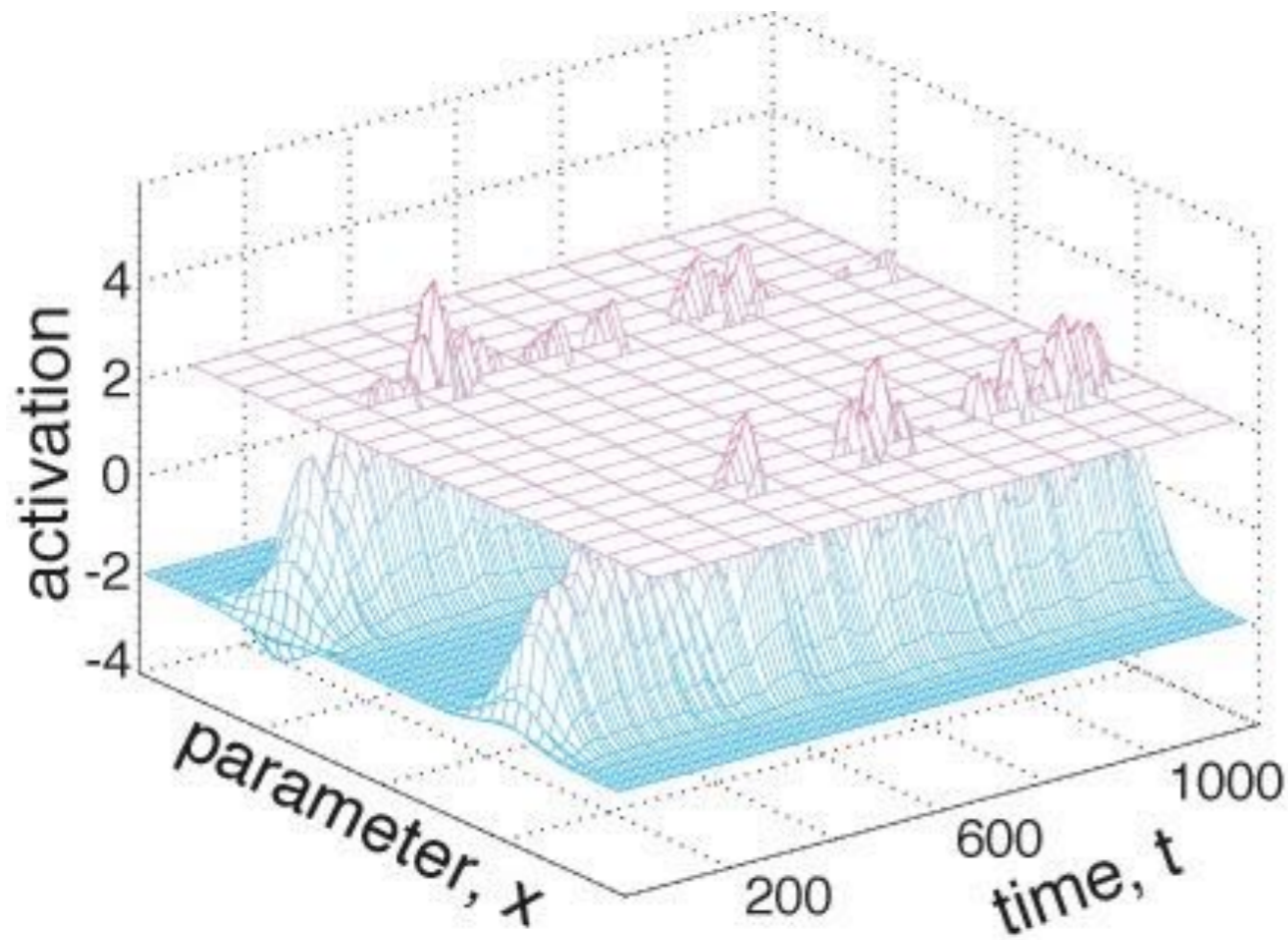
Detection instability



selection instability



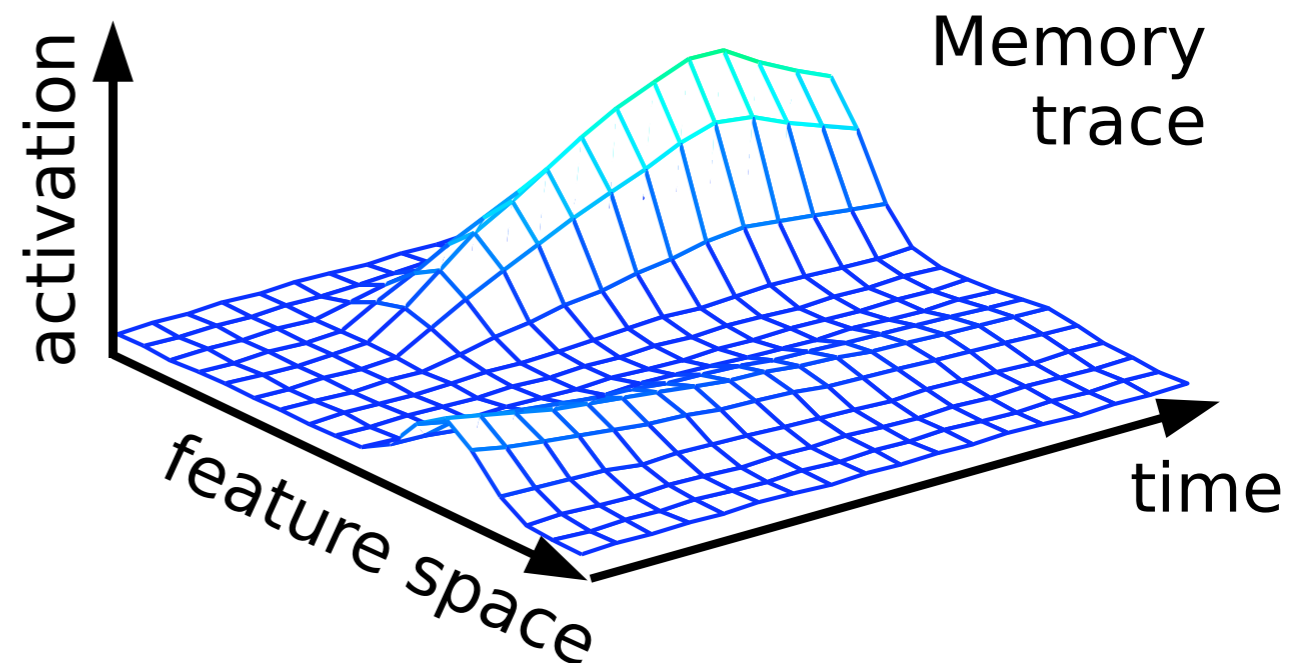
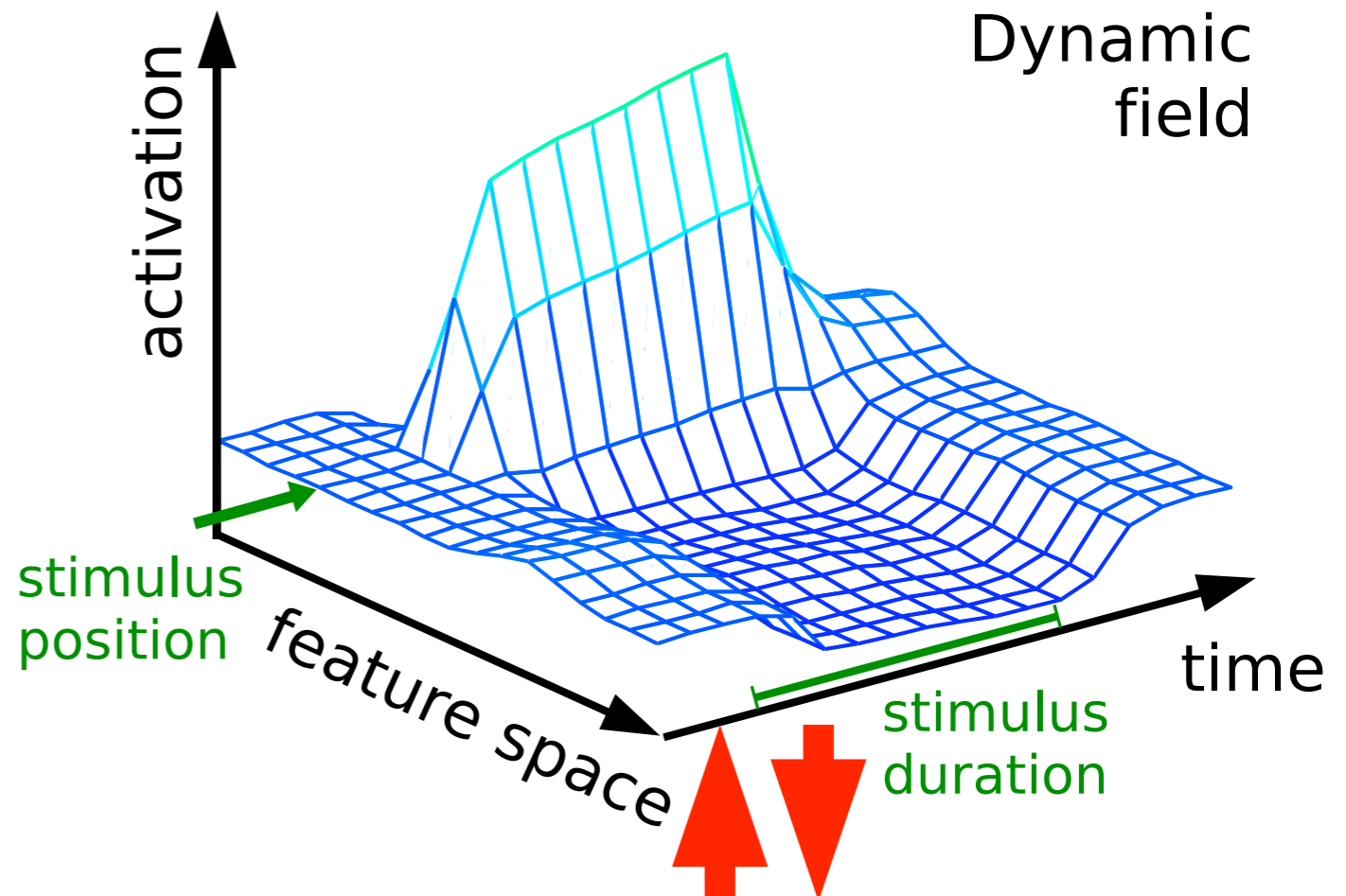
Stabilizing selection decisions

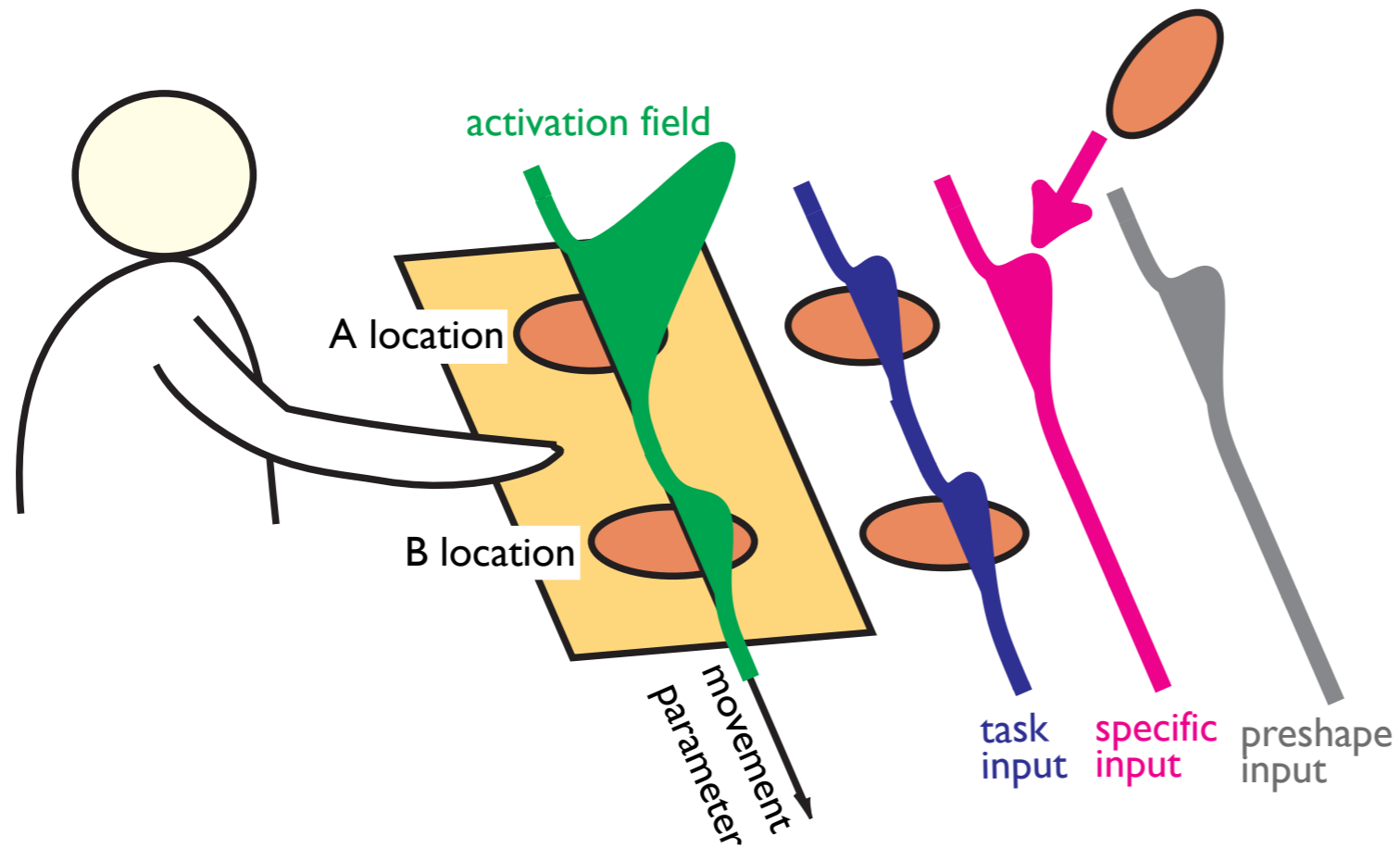


[Wilimzig, Schöner, 2006]

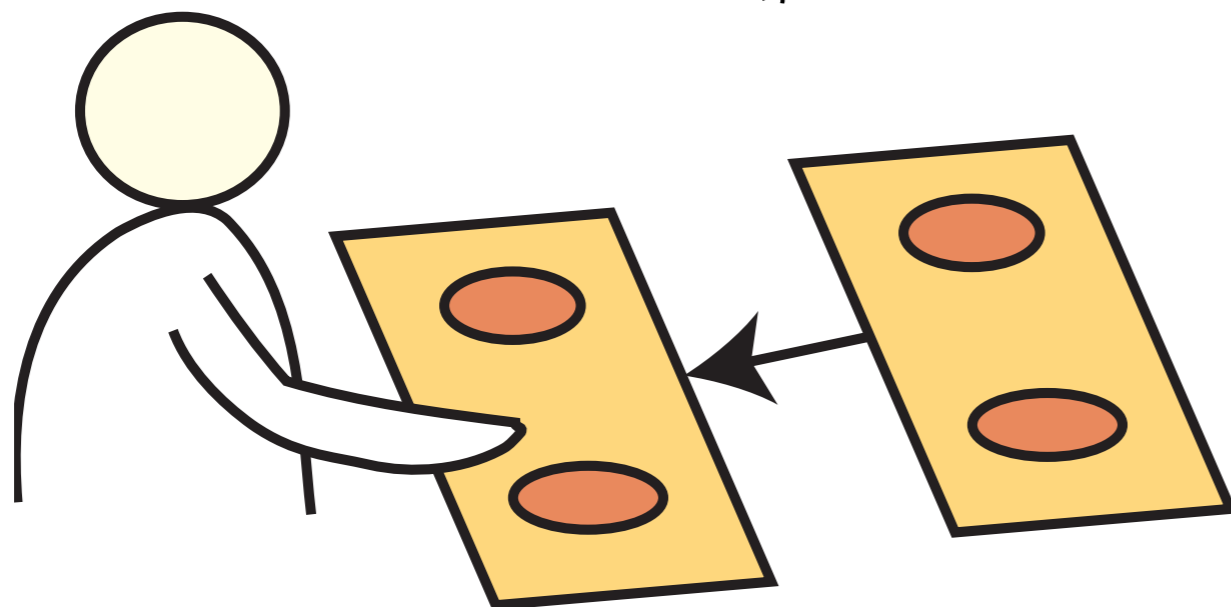
The memory trace

- activation leaves a trace that may influence the activation dynamics later...
- a simplest form of learning
- relevant in DFT because the detection instability may amplify the slightly inhomogeneous activation patterns induced by the memory trace into peaks of activation





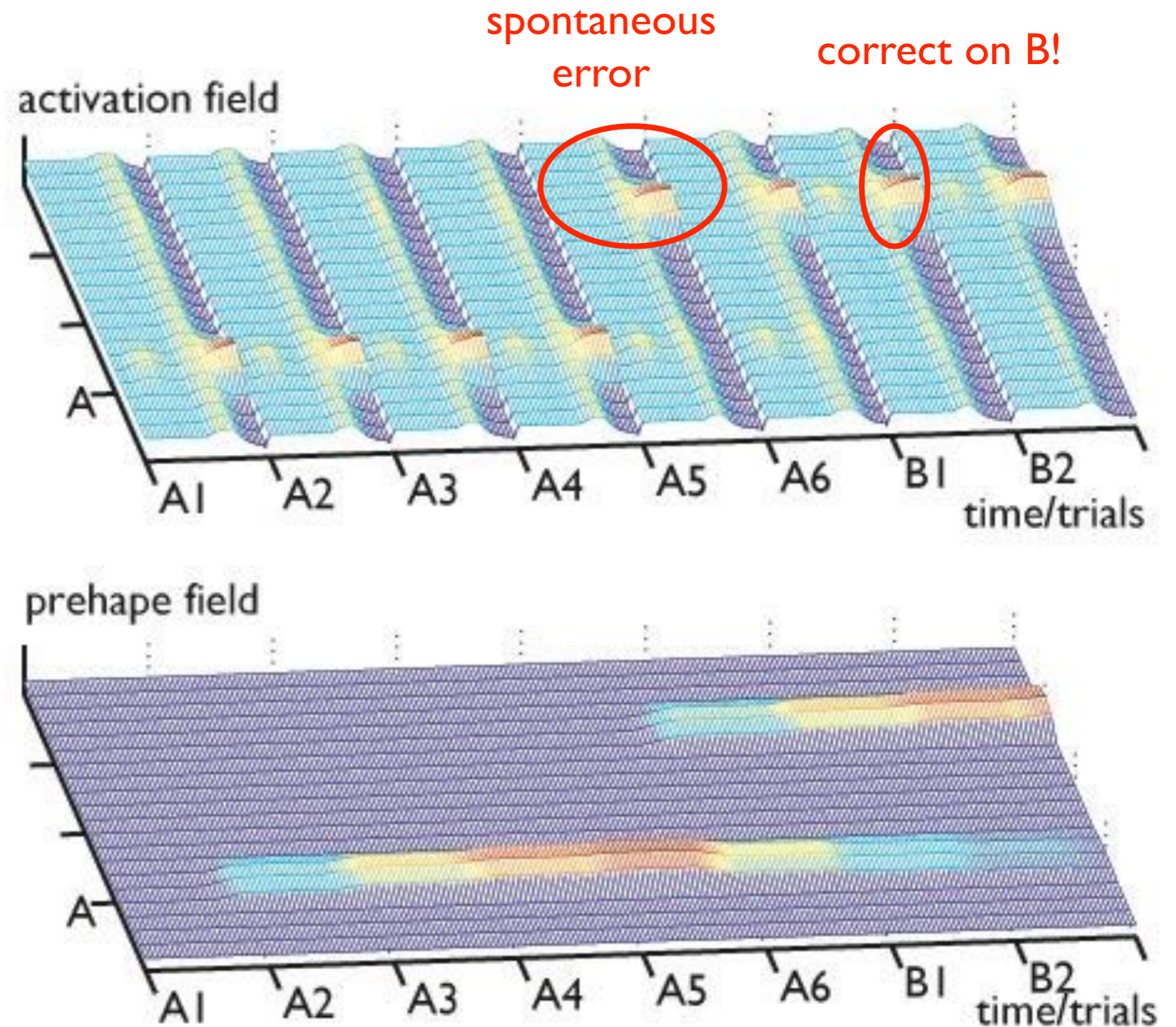
[Thelen, et al., BBS (2001)]



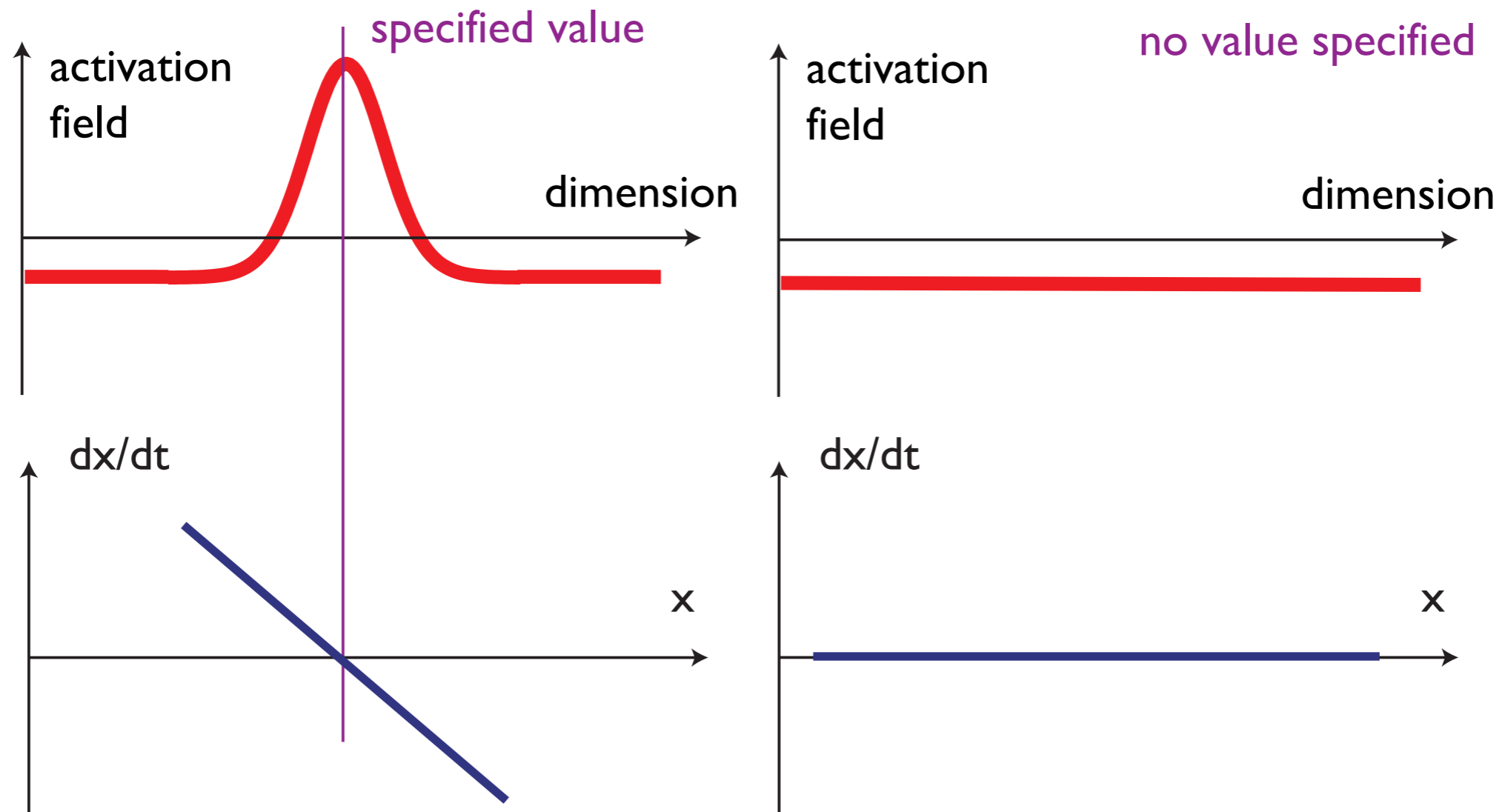
[Dinveva, Schöner, Dev. Science 2007]

DFT of infant perseverative reaching

- that is because reaches to B on A trials leave memory trace at B



From neural to behavioral dynamics



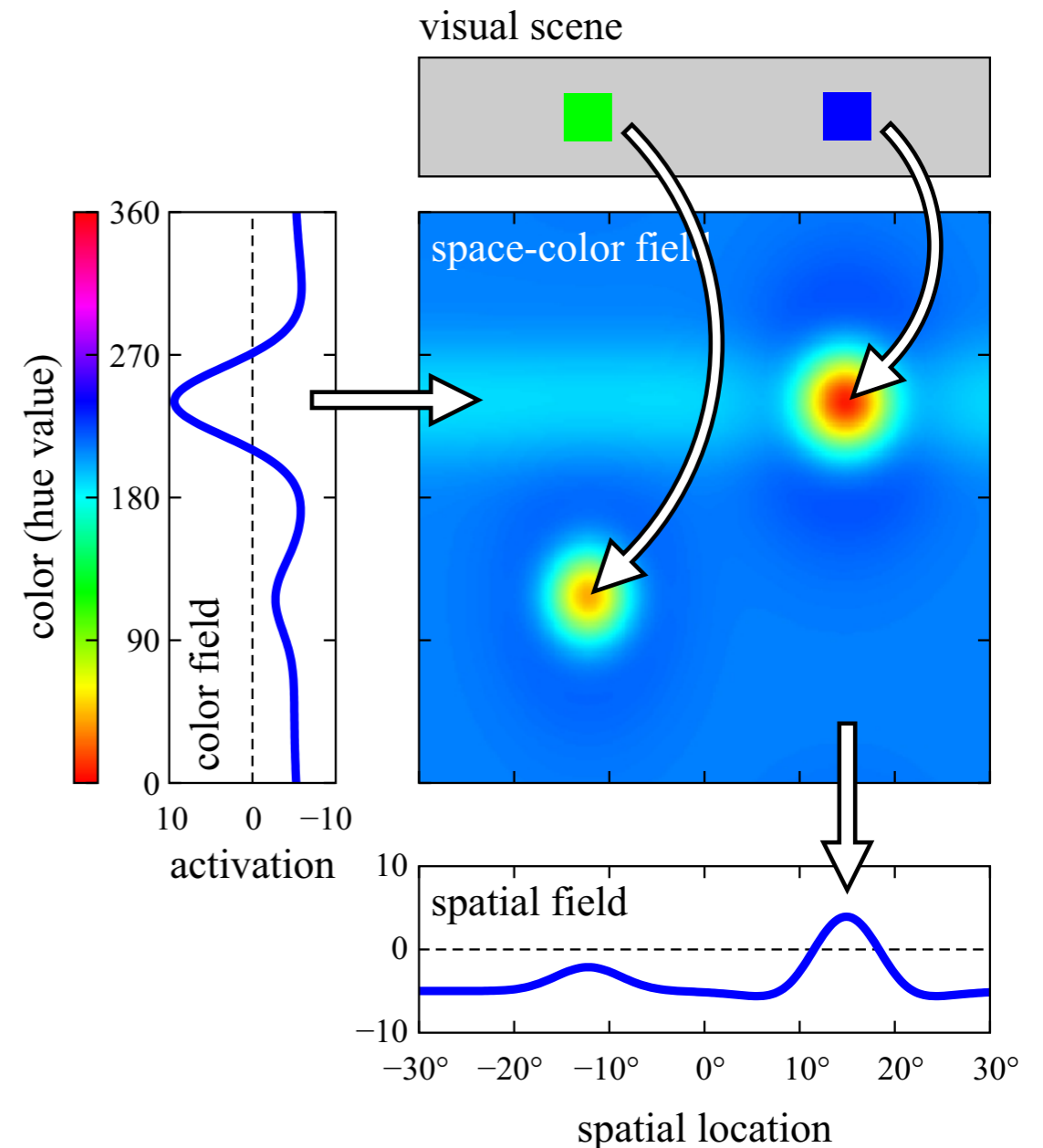
$$x_{\text{peak}} = \frac{\int dx \, x \, \sigma(u(x, t))}{\int dx \, \sigma(u(x, t))}$$

$$\dot{x} = - \left[\int dx \, \sigma(u(x, t)) \right] (x - x_{\text{peak}})$$

$$\Rightarrow \dot{x} = - \left[\int dx \, \sigma(u(x, t)) \right] x + \left[\int dx \, x \, \sigma(u(x, t)) \right]$$

New functions from higher-dimensional fields

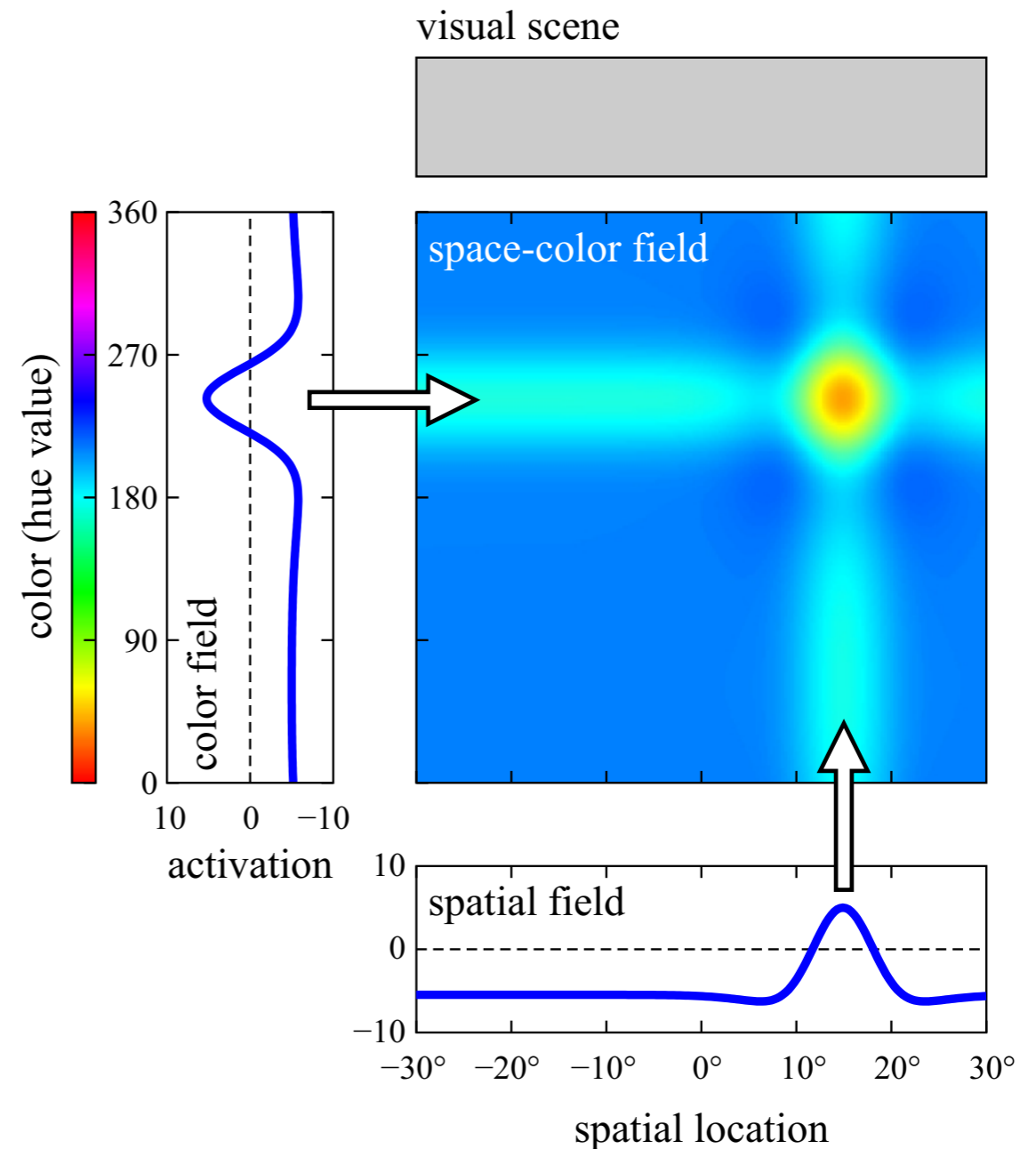
- visual search: combine ridge input with 2D input..



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

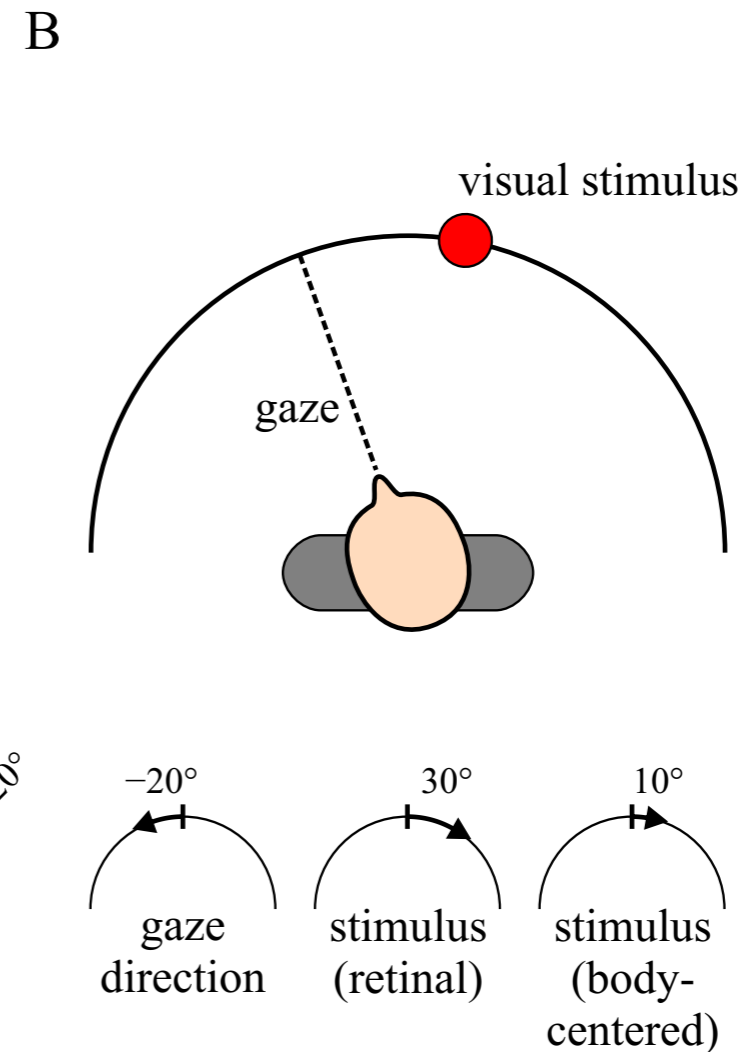
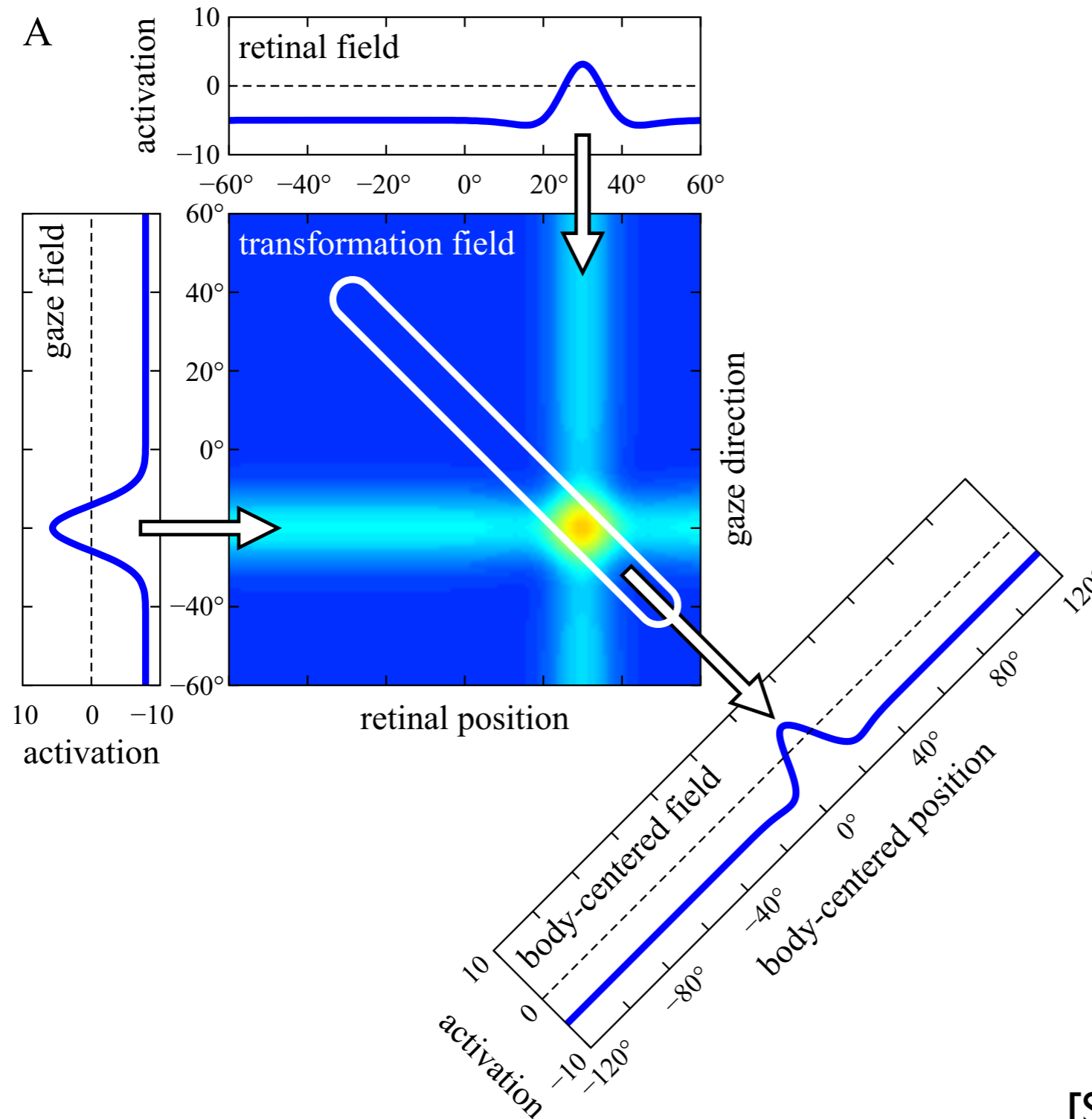
New functions from higher-dimensional fields

- peaks at intersections of ridges: bind two dimensions



[Slides adapted from Sebastian Schneegans, see Schneegans, Lins, Spencer, Chapter 5 of Dynamic Field Theory-A Primer, OUP, 2015]

New functions from higher-dimensional fields: coordinate transforms



[Slides adapted from Sebastian Schneegans, see Schneegans, Chapter 7 of Dynamic Field Theory-A Primer, OUP, 2015]

Toward higher cognition: Grounding spatial concepts

- bring objects into foreground
- make coordinate transformation
- apply comparison operators

