## Navigation

Gregor Schöner
May 2022

## Problem

we talked about how to plan motion toward targets avoiding obstacles

- in many cases, information about targets may be available through a map that represents where relevant locations are in the world
$\square$ to use a map, a robot/organism needs to known "where it is" on the map: egolocation estimation
$\square$ that estimate must be updated as a robot/ organism moves...


## Dead-reckoning/path integration

$\square$ if the agent knows its current velocity=heading direction + speed (and keeps track of time), it can estimate its change of position by integration

[McNaughton et al., Nature reviews neuroscience 2006]

## Dead-reckoning/path integration

a long history in technology... dating back to literal "navigation": sailing ships...
$\square$ estimating heading direction based on a compass
$\square$ estimating speed by counting "knots"... which entails an estimate of time
$\square$ updating position in a map

## Dead-reckoning/path integration

$\square$ modern technology increases the precision
$\square$ e.g. inertial guidance by measuring acceleration
$\square$ precise measurement of time
$\square$ with good control, the control signals can also be used to predict the new state ...
$\square$ optimal estimation integrates prediction and measurement...

## Dead-reckoning/path integration

## $\square$ fundamental problem

the integration leads to an accumulation of uncertainty...
$\square$ the principle of Brownian motion...


## Dead-reckoning/path integration

$\square$ a need for "recalibration" or re-setting of the estimate.. based on "recognizing" the true location on the map...
$\square$ historical solution:

- landmark recognition...
$\square$ triangulation
modern variants based on special beacons, GPS etc


## Dead-reckoning/path integration

$\square$ animals including humans use path integration

[Loomis, Klatzky, 1993]

## Dead-reckoning/path integration

## $\square$ animals including humans use path integration


blind from birth

blind from accident
seeing

## Landmark recognition

$\square$ landmarks are not necessarily objects...
$\square$ empirical evidence that views serve to estimate ego-position and pose
$\square$ evidence for views used from animal behavior and neural data

A Experimental environment $\therefore \underset{\text { Mountains }}{s A n}$


B Experimental tasks

Environmental learning Object viewing


Judgment of Relative Direction
\#=+Guitar@^*
Facing \#=Umbrella^*
\#=+.Tree(@ ${ }^{\wedge *}$ ?


Distance comparison
Free recall


C Experimental procedure


## Maps

when can we say does an animal use a map?
rather than use stimulus-response chaining
$\square=>$ when it can take short-cuts

[Peer et al, 2020]
[Poucet, I993]

## SLAM

- Simultaneous Localization and Mapping

[Durrant-Whyte, Baily, 2006]


## SLAM

problem of learning/optimizing path integration... and using this to associated landmark information with locations

- problem of loop closure



## (Neural) dynamics of navigation

dynamics for ego-position estimation
dynamical approach to learning the map: network of locations (home bases) at which the agent knows where it is relative to others
$\square$ dynamics of path planning

Self-calibration based on invariant view recognition:
Dynamic approach to navigation

## Neural and behavioral architecture



## Visual place navigation

$\square$
a visual surround (unsegmented) acquired in clusters around particular locations (home bases)
$\square$ views are stored together with current position estimate (translation/rotation)

Sample environment


## Evidence for home bases

$\square$ animals in given terrain build home bases by rearing in locations where they spend most of their time

| 7 | $7^{\prime}$ | 0 | $0^{\prime \prime}$ | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $6^{\prime}$ | $7^{\prime \prime}$ | $0^{\prime \prime}$ | $1^{\prime \prime}$ | $1^{\prime}$ |
| 6 | $6^{\prime \prime}$ | $C$ | $2^{\prime \prime}$ | 2 |
| $5^{\prime}$ | $5^{\prime \prime}$ | $4^{\prime \prime}$ | $3^{\prime \prime}$ | $2^{\prime \prime}$ |
| 5 | $4^{\prime \prime}$ | 4 | $3^{\prime \prime}$ | 3 |


[Eilam, Golani, 1989]

## Visual place navigation

$\square$ Each view in home base is matched to current view.... with all possible rotations actively generated from memorized view


## Visual place navigation

$\square$ Correlation function across rotation angle peaks sharply at true angular orientation of agent, even if translatior is not precise...
$\square$ so that estimation of orientation is possible while agent is in recepti field of place cell


## Visual place navigation

Correlation with actively shifted memory views decays spatially in way that reflects how distal the view is.... place field..


scale: 5



## Visual place navigation

The level of correlation across multiple views within a home base generates a place view representation of translation => position estimate

Place-cell like spatial view representation


## Neural and behavioral architecture



## Integration by an attractor dynamics

$\square$ every sensory estimate contributes a "force-let" to a dynamical system whose attractor is the estimate of ego-position
$\square$ for vision: space to rate code... removes the problem of normalization


## Recalibration from instability


with visual match, a strong attractor force-let induces instability in which the estimate gets reset to the visually specified estimate


which resets the dead-reckoned estimate as well

## Recalibration

 from instability$\square$ with visual match, a strong attractor force-let induces instability in which the estimate gets reset to the visually specified estimate
which resets the dead-reckoned estimate as well
no visual estimate



## Neural and behavioral architecture



## Integrating it all: dynamics all the



## a reset event



Visual match for home base recognition


Relaxation times (solid: tau_int,vis dashed: tau_int,dr dotted: tau_dr)


## Further development:

© complex behavioral organization
robotic implementation

## Autonomous behavioral organization

neural dynamics organizes sequence of behaviors...


## Autonomous behavioral organization

■ neural dynamics organizes sequence of behaviors...


## How neurally realistic is this?

## Neural mechanisms of navigation

neural representation of path integration

[McNaughton et al., Nature reviews neuroscience 2006]

## Heading direction

$\square$ Neural evidence for head-orientation cells... that function as heading direction representation

- Neural attractor dynamics (neural field) for heading direction

[McNaughton et al., Nature reviews neuroscience 2006]


## Place and grid cells

$\square$ neural representation of location in Hippocampus and Entorhinal Cortex
a

[McNaughton et al., Nature reviews neuroscience 2006]
b


## Place and grid cells

$\square$ support building a place representation by a neural field

[McNaughton et al.,
Nature reviews neuroscience 2006]

## Neural dynamics of path integration



No motion

[McNaughton et al., Nature reviews neuroscience 2006]

## Neural dynamics of path integration


[McNaughton et al., Nature reviews neuroscience 2006]

## Neurally inspired technical solution


[Ball,Wyeth, Cork, Milford, 20I3]

## RAT-Slam


[Ball,Wyeth, Cork, Milford, 20I3]

## RAT-Slam


[Ball,Wyeth, Cork, Milford, 20I3]

## RAT-Slam


(b)

[Ball,Wyeth, Cork, Milford, 20I3]

## Event-based place recognition

$\square$ spiking neural vision system...


Fig. 8: Example matches of the ensemble and ground-truth (GT) matches on the DDD-17 dataset. Top two rows: success cases where the majority of individual methods failed. Bottom two rows: failure cases.
[Fischer Mildord, 2020]

## Neuromorphic head-direction estimate

using DFT

[Kreiser et al. Sandamirskaya, Frontiers 2019]

# Neuromorphic head-direction estimate 

$\square$ using DFT

[Kreiser et al. Sandamirskaya, Frontiers 2019]

## Conclusions

$\square$ the navigation problem entails both knowing where you are and how to go places
$\square$ navigation can be performed by behavioral and neural dynamics

- recalibration of location based on recognition ... can be view-based

■ integration by (neural) dynamics ... in which space-time continuous processes... lead to discrete transitions at instabilities

