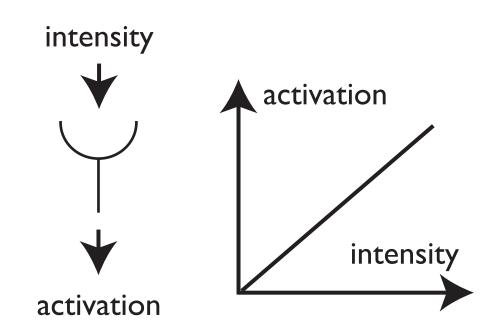
Neural Dynamics

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Sensors

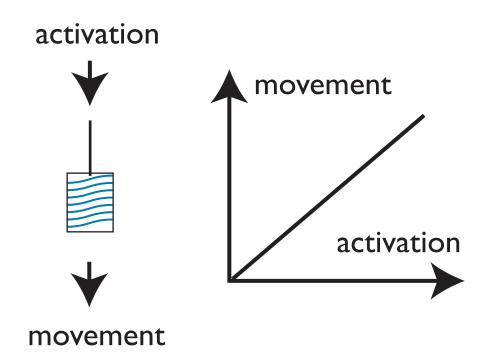
- transform a physical intensity into a neural activation
- intensity: light, sound, displacement
- neural activation: membrane potential, spike rate



Motors

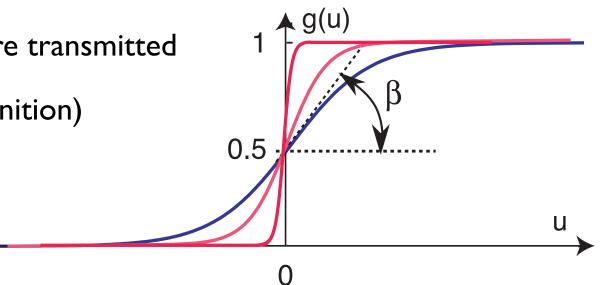
transform activation into physical action

… muscles



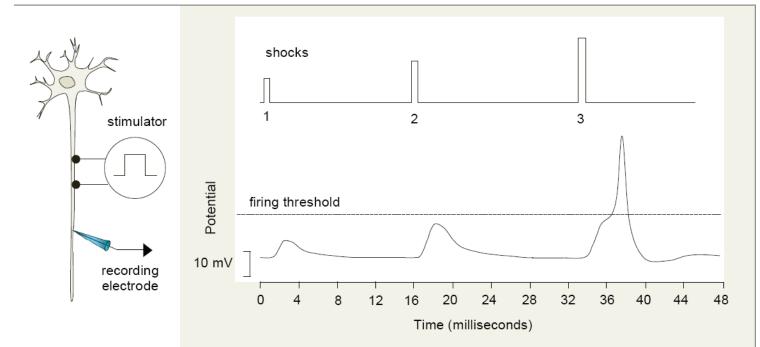
What is "activation"?

- activation is an abstraction of the state of neurons, defined relative to sigmoidal threshold function
 - Iow levels of activation are not transmitted (to other neural systems, to motor systems)
 - high levels of activation are transmitted
 - threshold at zero (by definition)



Origin of the activation concept in neurophysics

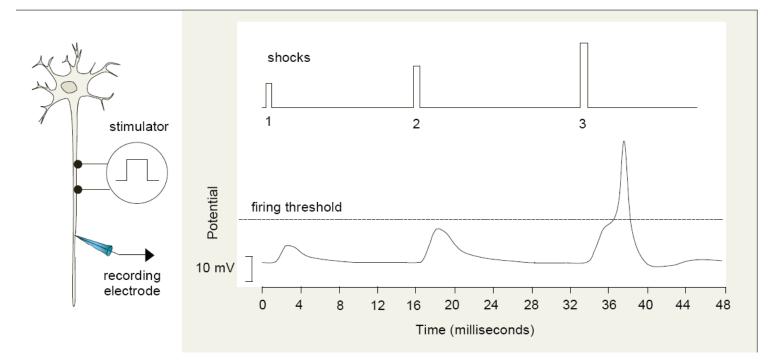
activation, u, as a real number that reflects the (population) membrane potential



[from: Tresilian, 2012]

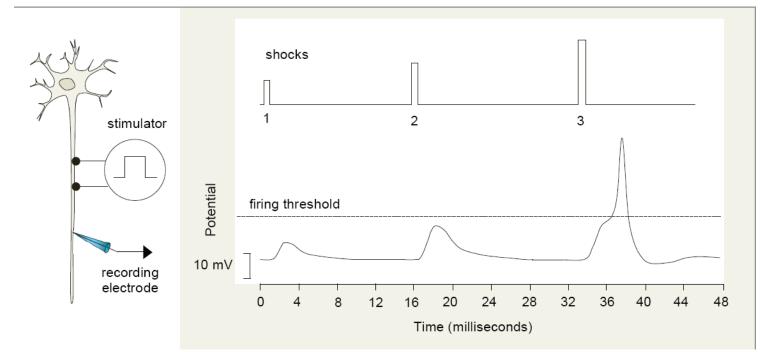
 \blacksquare u(t) evolves as a dynamical system, characterized by a time scale, $\tau \approx 10 \mathrm{ms}$

 $\tau \dot{u}(t) = -u(t) + h + \operatorname{input}(t)$



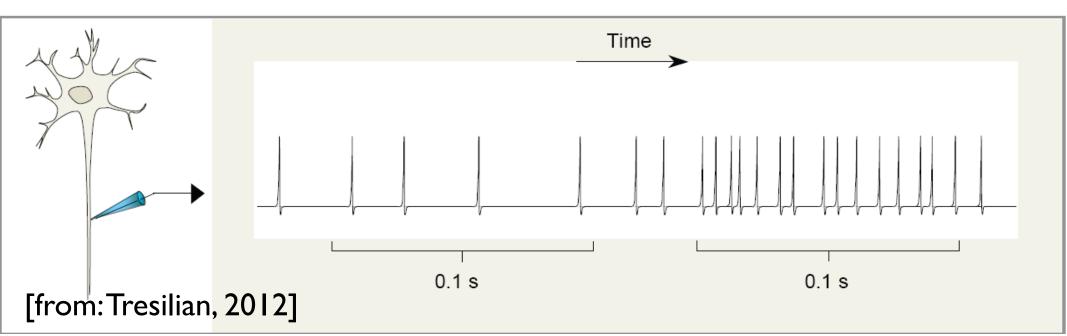
[from: Tresilian, 2012]

- spiking when membrane potential exceeds threshold....
- spike train is transmitted to downstream neurons

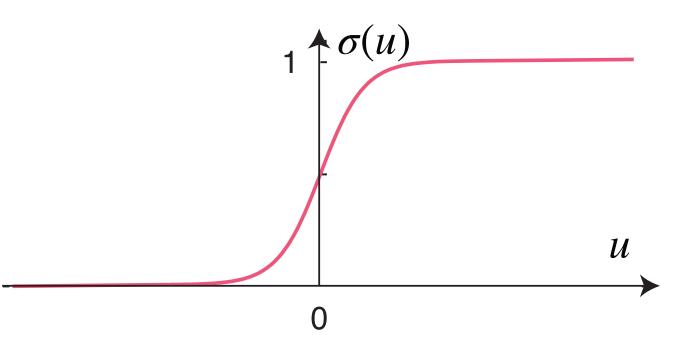


[from: Tresilian, 2012]

activation captures different firing rates in a small population...



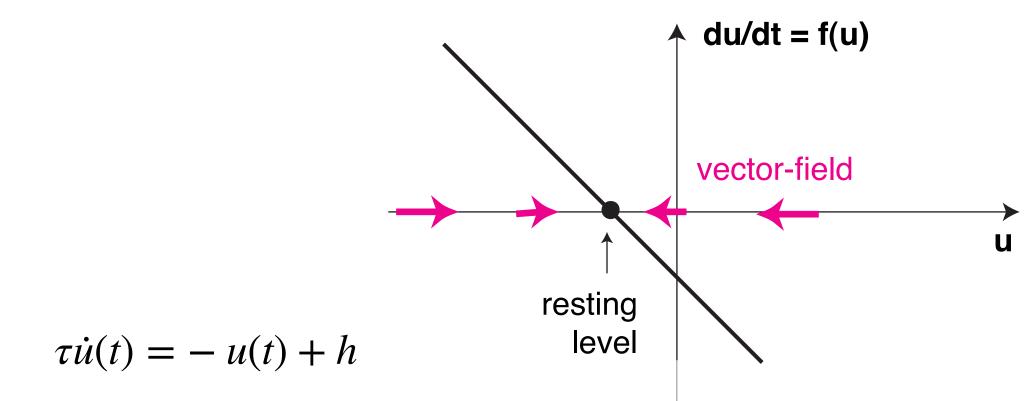
in neural dynamics, the spiking mechanism and associated firing rate is replaced by a statistical (population) description: threshold function



Neural dynamics

dynamical system: the present predicts the future

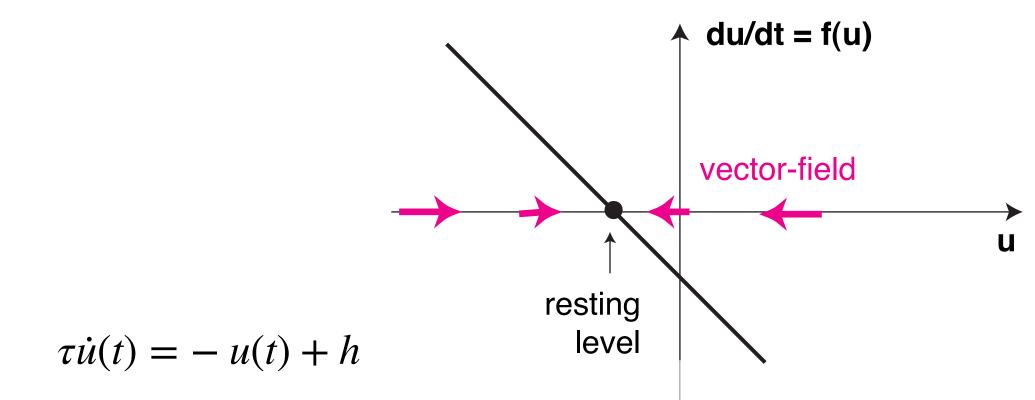
given a initial level of activation, u(0), the activation, u(t), at times t>0 is uniquely determined



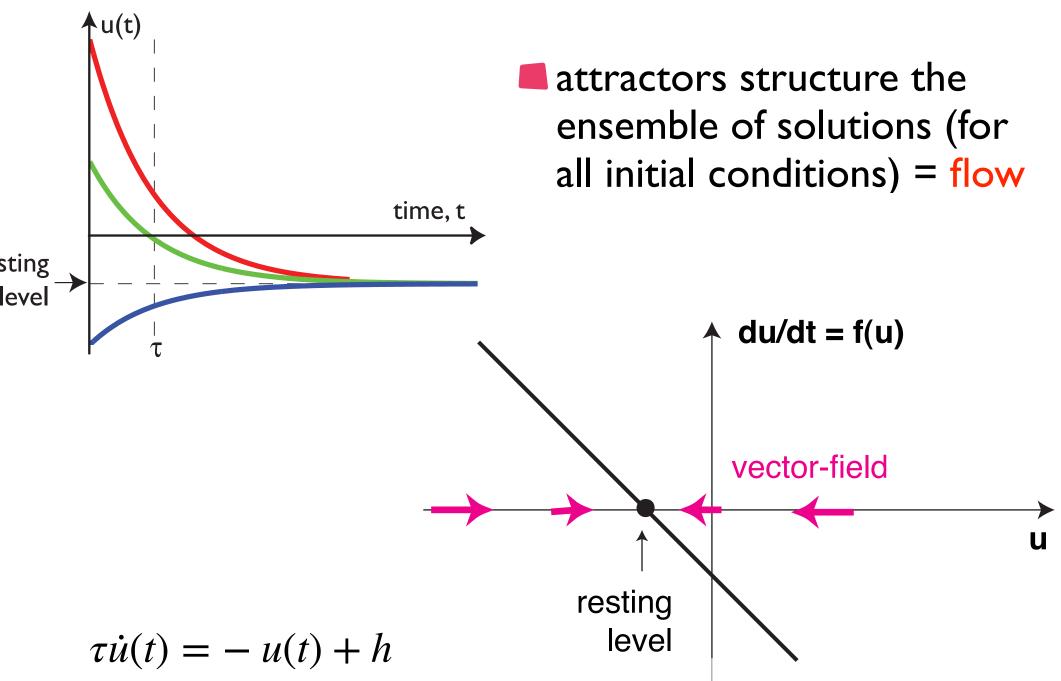
Neural dynamics

fixed point = constant solution (stationary state)

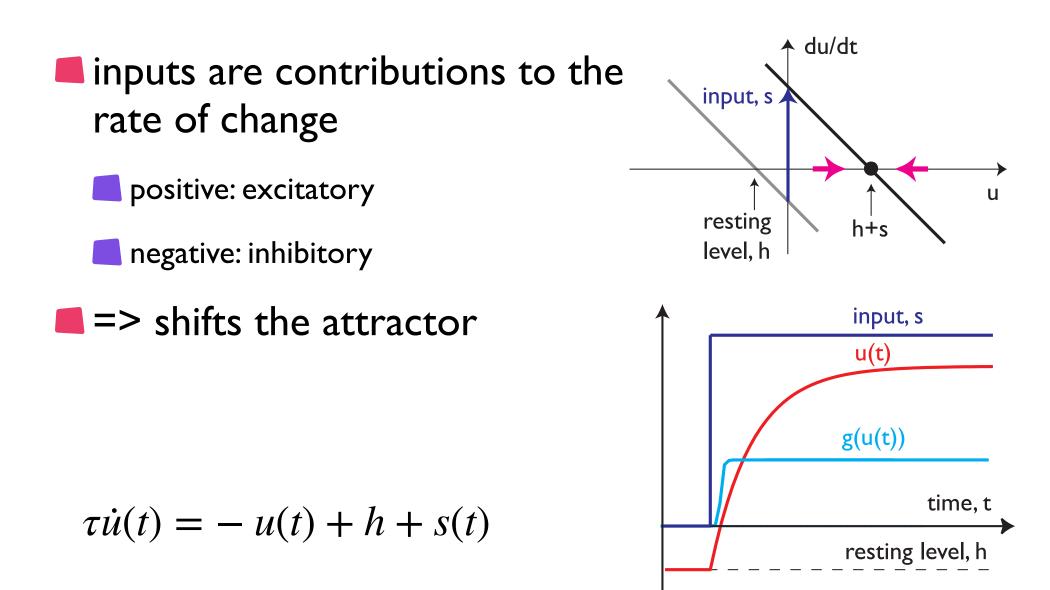
stable fixed point = attractor: nearby solutions converge to the fixed point



Neural dynamics



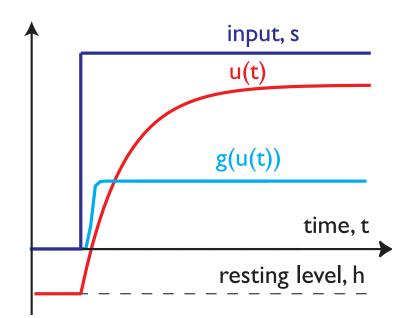
Neuronal dynamics



Neuronal dynamics

- what is transmitted is $\sigma(u(t))$
- (labelled g(t) in the book and in some figures)
- neural dynamics as a lowpass filter of time varying input
- = input-driven solution

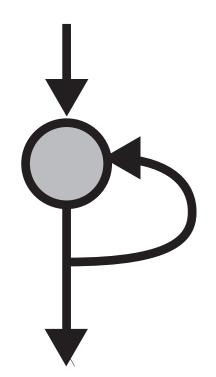
$$\tau \dot{u}(t) = -u(t) + h + s(t)$$



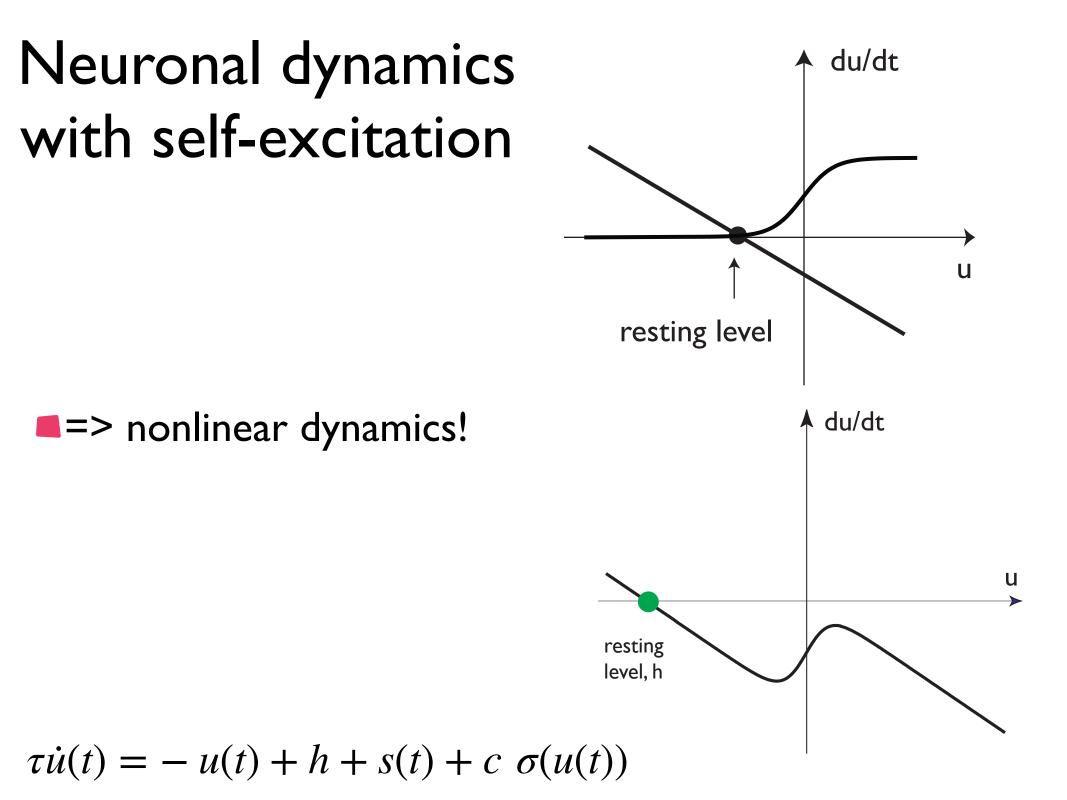
=> simulation

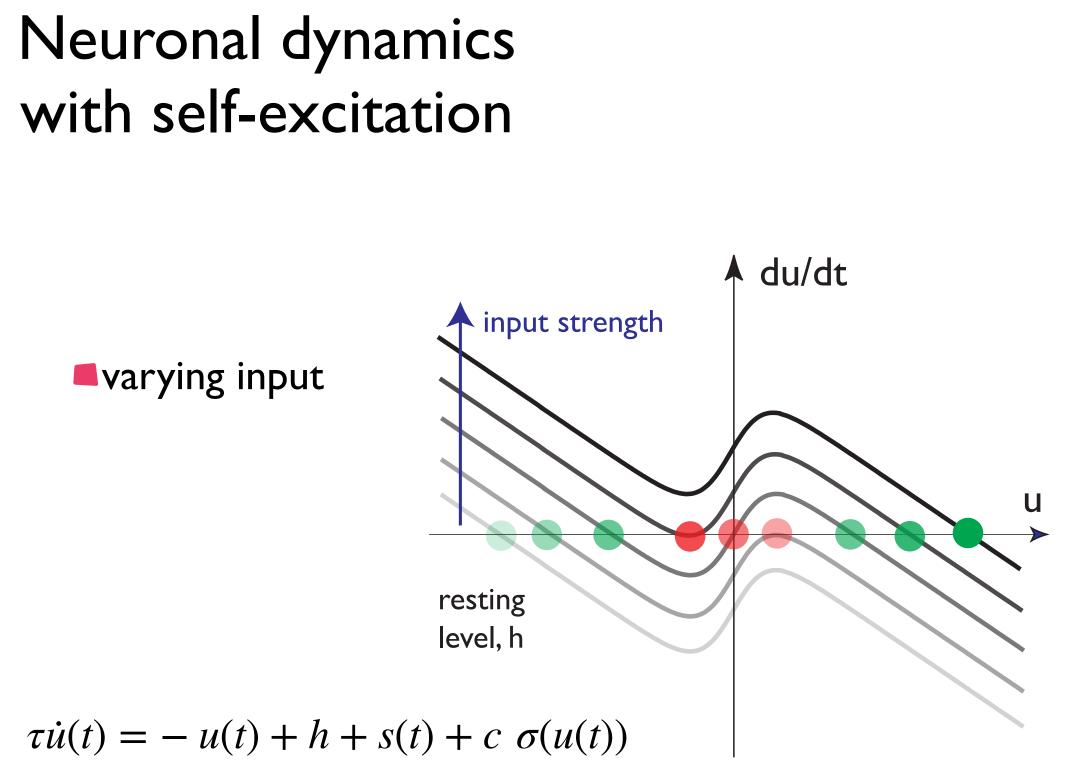
Neuronal dynamics with self-excitation

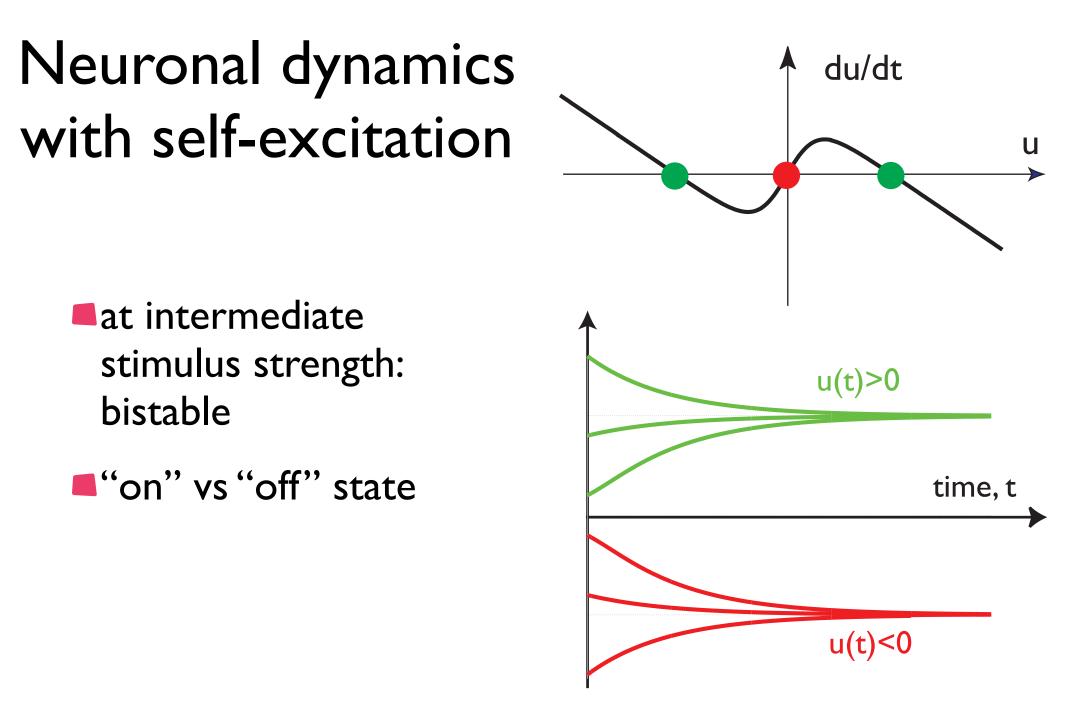
activation variable with selfexcitation (representing a small population with excitatory coupling)



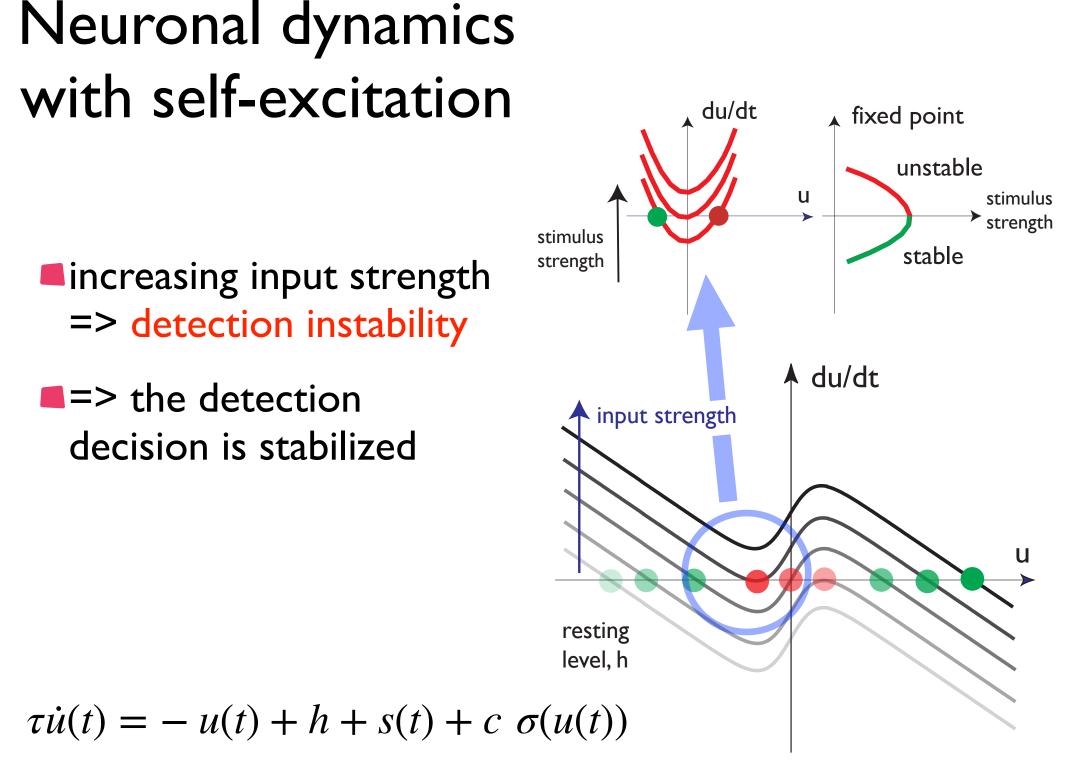
 $\tau \dot{u}(t) = -u(t) + h + s(t) + c \ \sigma(u(t))$

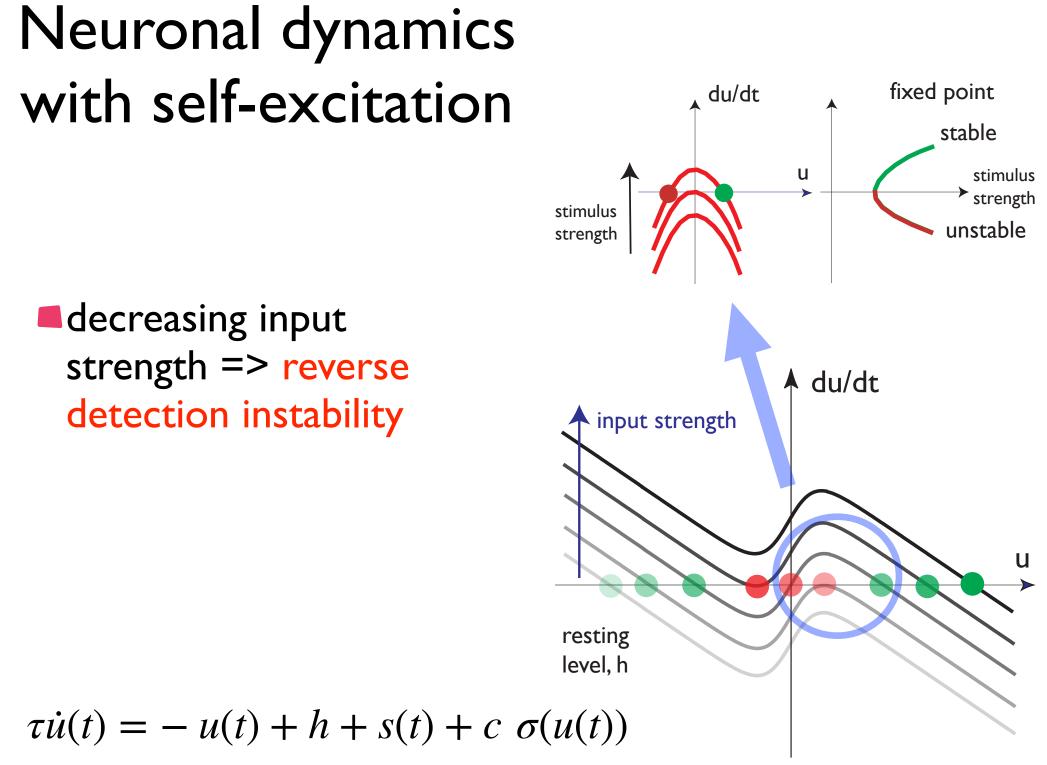






 $\tau \dot{u}(t) = -u(t) + h + s(t) + c \ \sigma(u(t))$

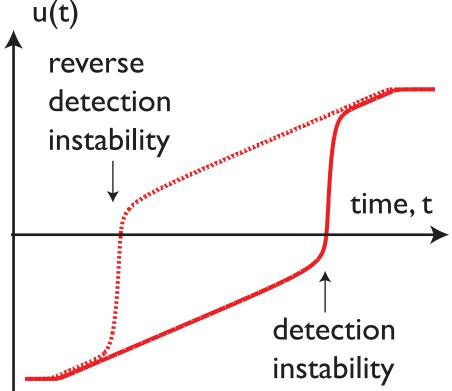




$$\tau \dot{u}(t) = -u(t) + h + s(t) + c \ \sigma(u(t))$$

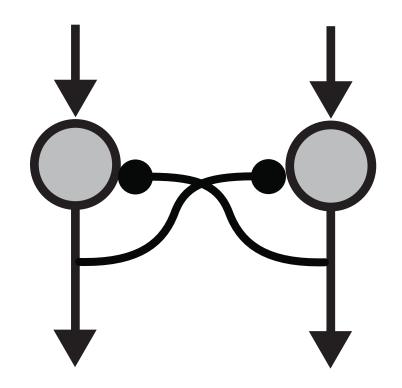
Neuronal dynamics with self-excitation

the detection and its reverse => create discrete events from time-continuous changes



=> simulation

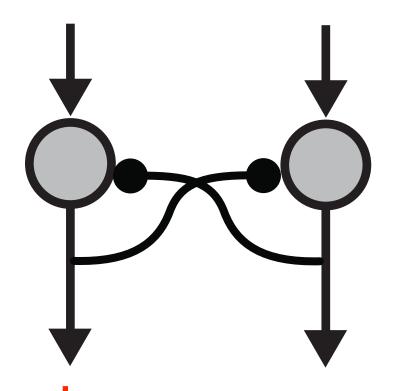
- two activation variables with reciprocal inhibitory coupling
- representing two small populations that are inhibitorily coupled



$$\tau \dot{u}_1(t) = -u_1(t) + h + s_1(t) - c_{12}\sigma(u_2(t))$$

$$\tau \dot{u}_2(t) = -u_2(t) + h + s_2(t) - c_{21}\sigma(u_1(t))$$

Coupling: the rate of change of one activation variable depends on the level of activation of the other activation variable

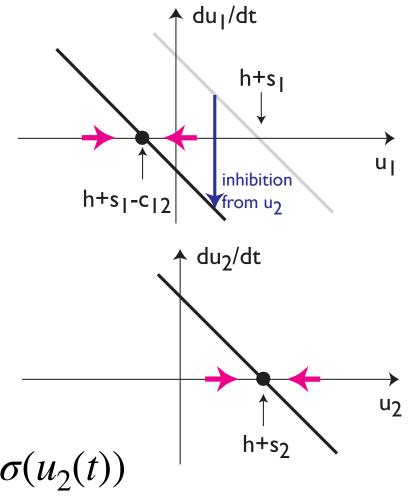


coupling

 $\tau \dot{u}_1(t) = -u_1(t) + h + s_1(t) - c_{12}\sigma(u_2(t))$ $\tau \dot{u}_2(t) = -u_2(t) + h + s_2(t) - c_{21}\sigma(u_1(t))$

to visualize, assume that u₂ has been activated by input to a positive level

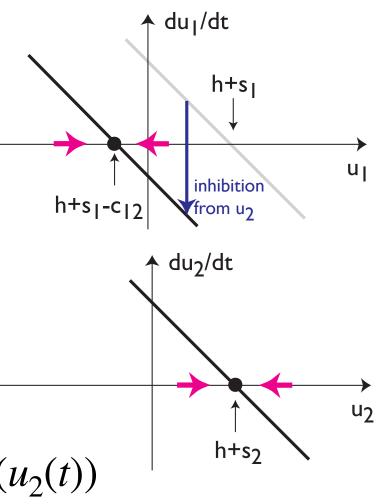
=> it inhibits u_1



 $\tau \dot{u}_1(t) = -u_1(t) + h + s_1(t) - c_{12}\sigma(u_2(t))$

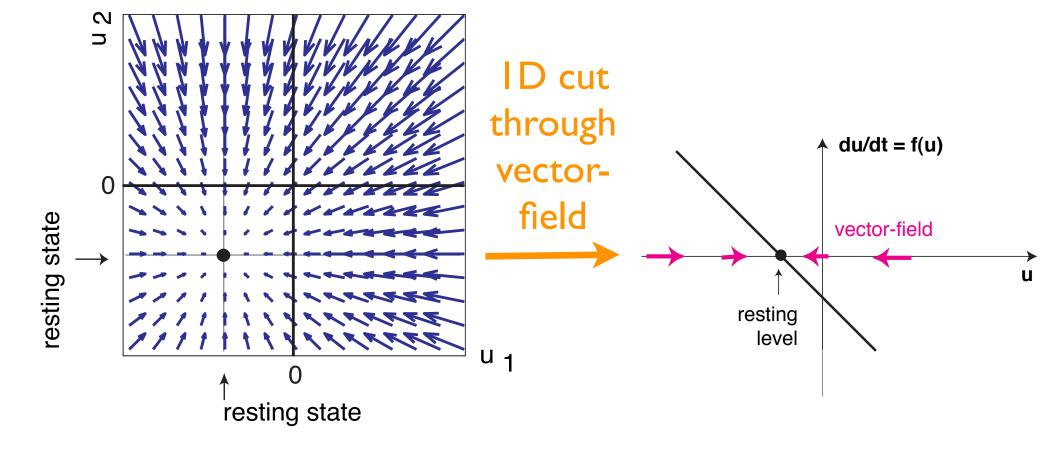
 $\tau \dot{u}_2(t) = -u_2(t) + h + s_2(t) - c_{21}\sigma(u_1(t))$

- why would u_2 be positive before u_1 ?
- more input to u₂ (better "match") => faster increase
- input advantage <=> time advantage <=> competitive advantage

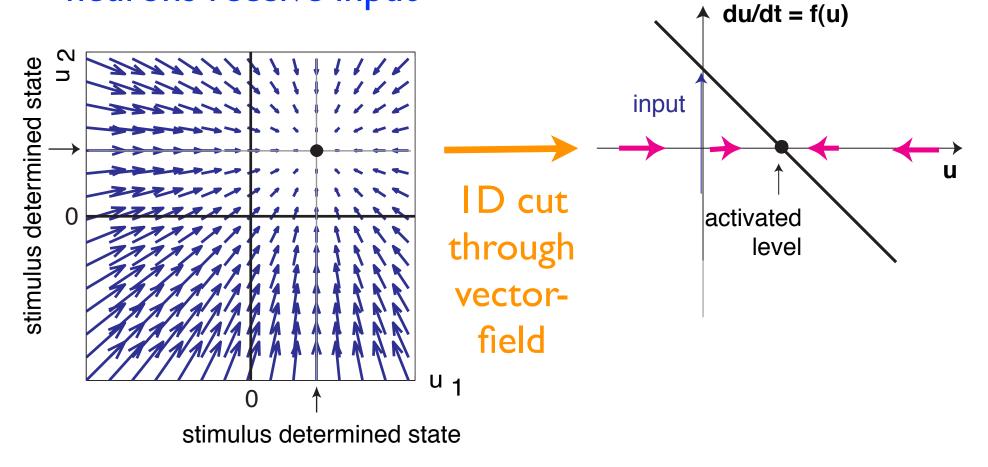


- $\tau \dot{u}_1(t) = -u_1(t) + h + s_1(t) c_{12}\sigma(u_2(t))$
- $\tau \dot{u}_2(t) = -u_2(t) + h + s_2(t) c_{21}\sigma(u_1(t))$

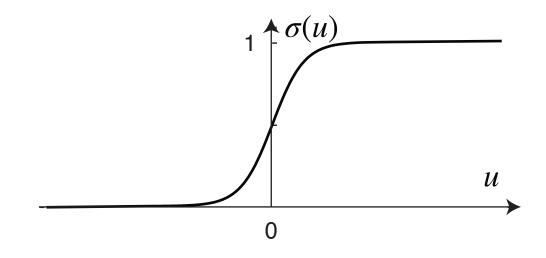




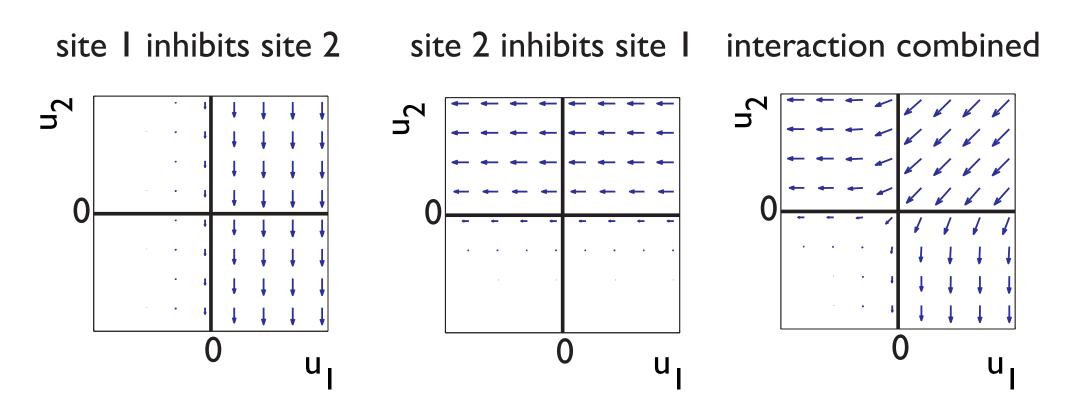
vector-field (without interaction) when both neurons receive input



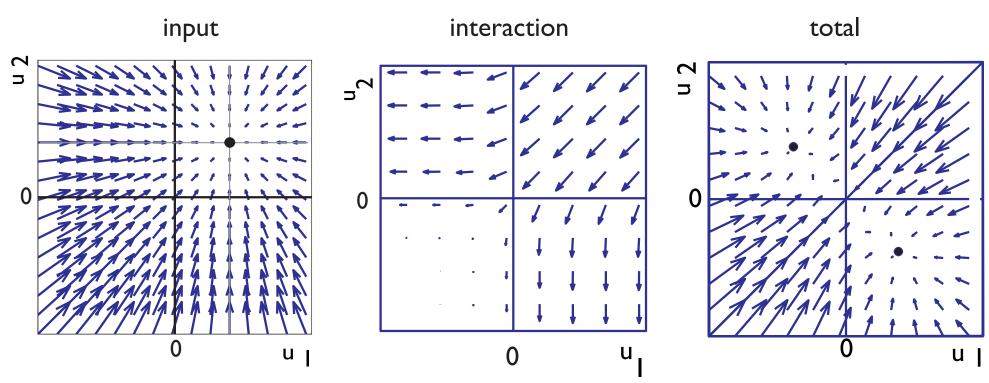
only activated neurons participate in interaction!

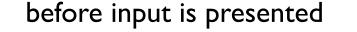


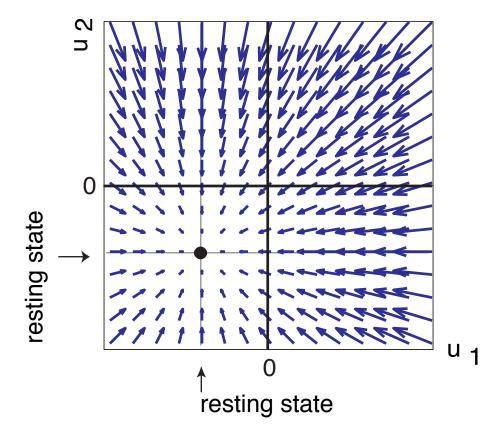
vector-field of mutual inhibition



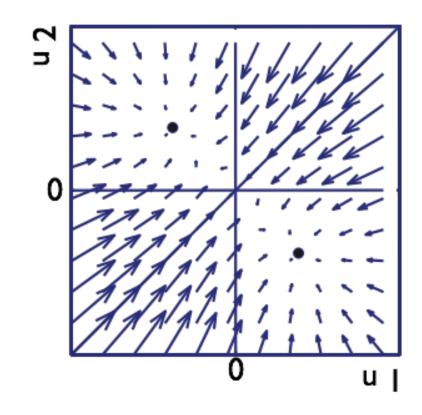
vector-field with strong mutual inhibition: bistable



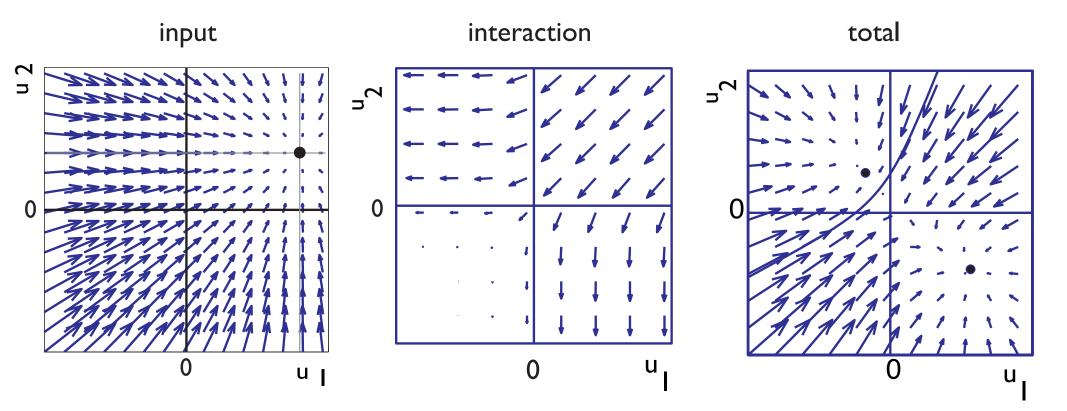




after input is presented



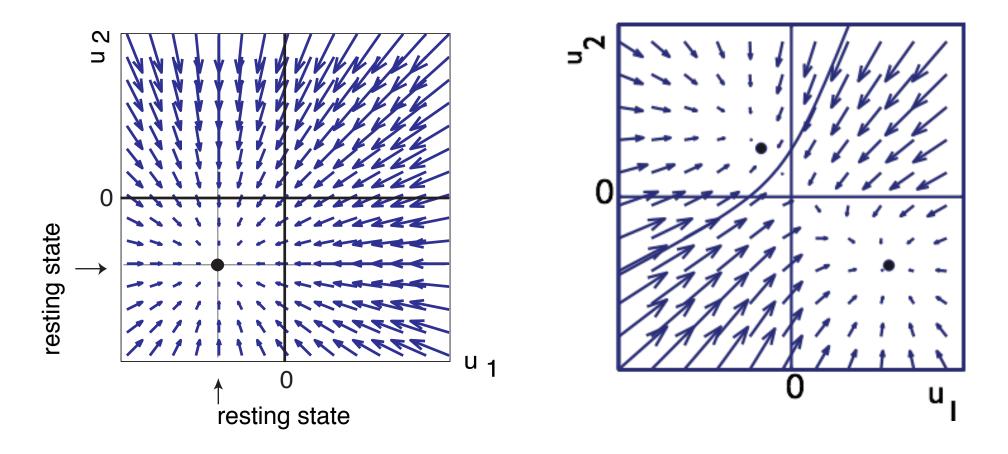
stronger input to $u_1 =>$ attractor with positive u_1 stronger, attractor with positive u_2 weaker => closer to instability



decision made at detection instability!

before input is presented

after input is presented



=> simulation

The neural dynamics of fields

- … the same underlying math
- coupling among continuously many activation variables
- Iocal excitatory coupling ("self-excitation")
- global inhibitory coupling ("mutual inhibition")

field vs. activation variables

